

SPARQL over RDF, and its possible extensions to RDFS

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- ▶ RDF and RDFS: A brief introduction
- ▶ SPARQL: A query language for RDF
 - ▶ Formal semantics
 - ▶ Complexity of the evaluation problem
 - ▶ Optimization methods
- ▶ SPARQL as a query language for RDFS
 - ▶ Formal semantics and the closure of an RDFS graph
- ▶ NAV-SPARQL: A navigational query language for RDFS

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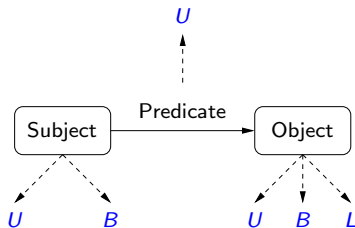
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RDF in a nutshell

- ▶ RDF is the W3C proposal framework for representing information in the Web.
- ▶ Abstract syntax based on directed labeled graph.
- ▶ Schema definition language (**RDFS**): Define new vocabulary (typing, inheritance of classes and properties).
- ▶ Formal semantics.

RDF formal model

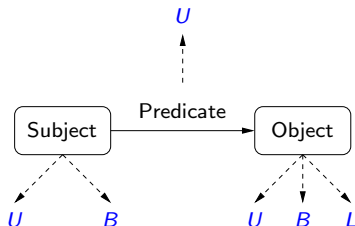


U = set of **U**ris

B = set of **B**lank nodes

L = set of **L**iterals

RDF formal model



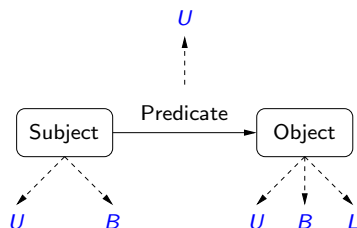
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$(s, p, o) \in (U \cup B) \times U \times (U \cup B \cup L)$ is called an **RDF triple**

RDF formal model



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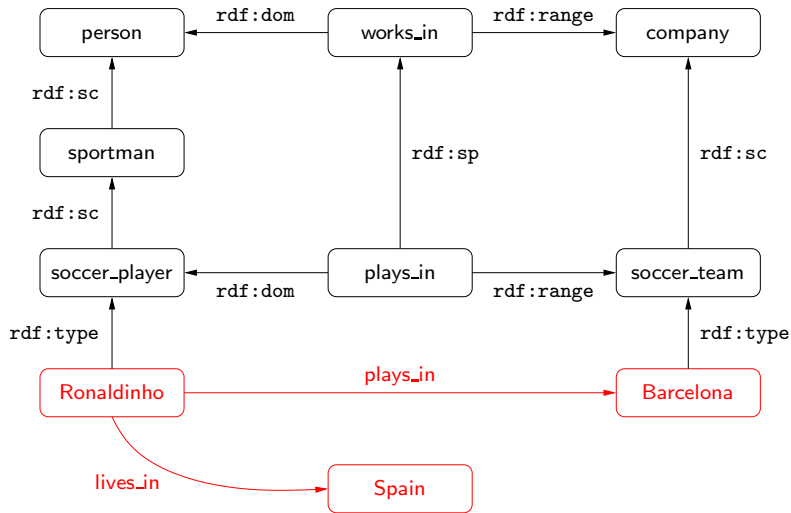
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A set of RDF triples is called an **RDF graph**

RDF: An example



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Querying RDF: SPARQL

- ▶ SPARQL is the W3C candidate recommendation query language for RDF.
- ▶ SPARQL is a graph-matching query language.
- ▶ A SPARQL query consists of three parts:
 - ▶ Pattern matching: optional, union, nesting, filtering.
 - ▶ Solution modifiers: projection, distinct, order, limit, offset.
 - ▶ Output part: construction of new triples, . . .

A simple RDF query language

```
SELECT ?Name ?Email
WHERE
{
  ?X :name ?Name
  ?X :email ?Email
}
```

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In general, in a query we have:

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- ▶ Head: processing of some variables.

A simple RDF query language

```
SELECT ?Name ?Email
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In general, in a query we have:

$$H \leftarrow P$$

- ▶ Head: processing of some variables.
- ▶ Body: pattern matching expression.

A simple RDF query language

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SELECT ?Name ?Email
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```

In general, in a query we have:

$$H \leftarrow P$$

- ▶ Head: processing of some variables.
- ▶ Body: pattern matching expression.

We focus on *P*.

But things can become more complex ...

Interesting features of pattern matching on graphs

- ▶ Grouping
- ▶ Optional parts
- ▶ Nesting
- ▶ Union of patterns
- ▶ Filtering

```
{ P1  
  P2 }
```

But things can become more complex ...

Interesting features of pattern matching on graphs

- ▶ **Grouping**
- ▶ Optional parts
- ▶ Nesting
- ▶ Union of patterns
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```
{ { P1  
  P2 }  
  
  { P3  
    P4 }  
  
}
```

But things can become more complex ...

Interesting features of pattern matching on graphs

- ▶ Grouping
- ▶ **Optional parts**
- ▶ Nesting
- ▶ Union of patterns
- ▶ Filtering

```
{ { P1
  P2
  OPTIONAL { P5 } }

{ P3
  P4
  OPTIONAL { P7 } }

}
```

But things can become more complex ...

Interesting features of pattern matching on graphs

- ▶ Grouping
- ▶ Optional parts
- ▶ **Nesting**
- ▶ Union of patterns
- ▶ Filtering

```
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{ P3
  P4
  OPTIONAL { P7
    OPTIONAL { P8 } } }
}
```

But things can become more complex ...

Interesting features of pattern matching on graphs

- ▶ Grouping
- ▶ Optional parts
- ▶ Nesting
- ▶ Union of patterns
- ▶ Filtering

```
{ { P1
  P2
  OPTIONAL { P5 } }

  { P3
    P4
    OPTIONAL { P7
      OPTIONAL { P8 } } }
}
```

UNION

```
{ P9 }
```

But things can become more complex ...

Interesting features of pattern matching on graphs

- ▶ Grouping
- ▶ Optional parts
- ▶ Nesting
- ▶ Union of patterns
- ▶ **Filtering**

```
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UNION
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  FILTER ( R ) }
```


A formal semantics for SPARQL

A formal approach would be beneficial for:

- ▶ Clarifying corner cases
- ▶ Helping in the implementation process
- ▶ Providing sound foundations

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In this presentation:

- ▶ A formal compositional semantics for SPARQL
- ▶ A study of the complexity of evaluating SPARQL
- ▶ Optimization procedures

A standard algebraic syntax

- ▶ Triple patterns: just triples + variables, **without blanks**

```
?X :name "john"
```

```
(?X, name, john)
```

- ▶ Graph patterns: full parenthesized algebra

```
{ P1 P2 }
```

```
( P1 AND P2 )
```

```
{ P1 OPTIONAL { P2 } }
```

```
( P1 OPT P2 )
```

```
{ P1 } UNION { P2 }
```

```
( P1 UNION P2 )
```

```
{ P1 FILTER ( R ) }
```

```
( P1 FILTER R )
```

original SPARQL syntax

algebraic syntax

A standard algebraic syntax

- ▶ **Explicit** precedence/association

Example

```
{ t1
  t2
  OPTIONAL { t3 }
  OPTIONAL { t4 }
  t5
}
```

$(((((t_1 \text{ AND } t_2) \text{ OPT } t_3) \text{ OPT } t_4) \text{ AND } t_5))$

Mappings: building block for the semantics

Definition

A mapping is a **partial function** from variables to RDF terms.

The evaluation of a pattern results in a set of mappings.

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The semantics of triple patterns

Given an RDF graph and a triple pattern t

Definition

The **evaluation** of t is the set of mappings that

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Example

graph	triple	evaluation						
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?X		?Y						
R_1		john						
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$(R_1, \text{email}, \text{J@ed.ex})$								
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?X	?Y					
R_1	john					
$(R_2, \text{name}, \text{paul})$		$\mu_2:$ <table border="1"><tr><td>?X</td><td>?Y</td></tr><tr><td>R_2</td><td>paul</td></tr></table>	?X	?Y	R_2	paul
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$?X$	$?Y$
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R_2	paul

Compatible mappings

Definition

Two mappings are **compatible** if they **agree** in their **shared variables**.

Example

	?X	?Y	?Z	?V
μ_1 :	R_1	john		
μ_2 :	R_1		J@edu.ex	
μ_3 :			P@edu.ex	R_2

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$\mu_1 \cup \mu_3$:	R_1	john	P@edu.ex	R_2

► μ_2 and μ_3 are not compatible

Sets of mappings and operations

Let M_1 and M_2 be sets of mappings:

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Join: $M_1 \bowtie M_2$

- ▶ extending mappings in M_1 with compatible mappings in M_2

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Let M_1 and M_2 be sets of mappings:

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- ▶ mappings in M_1 plus mappings in M_2 (set theoretical union)

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Definition

Left Outer Join: $M_1 \bowtie\! \bowtie M_2 = (M_1 \bowtie M_2) \cup (M_1 \setminus M_2)$

Semantics of SPARQL operators

Let M_1 and M_2 be the result of **evaluating** P_1 and P_2 .

Definition

The evaluation of:

$(P_1 \text{ AND } P_2)$	\rightarrow
$(P_1 \text{ UNION } P_2)$	\rightarrow
$(P_1 \text{ OPT } P_2)$	\rightarrow

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Simple example

Example

$(R_1, \text{name}, \text{john})$
 $(R_1, \text{email}, \text{J@ed.ex})$
 $(R_2, \text{name}, \text{paul})$

$((?X, \text{name}, ?Y) \text{ OPT } (?X, \text{email}, ?E))$

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► from the **Join**

Simple example

Example

$(R_1, \text{name}, \text{john})$
 $(R_1, \text{email}, \text{J@ed.ex})$
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$((?X, \text{name}, ?Y) \text{ OPT } (?X, \text{email}, ?E))$

?X	?Y
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?X	?E
R_1	J@ed.ex

► from the **Difference**

Simple example

Example

$(R_1, \text{name}, \text{john})$
 $(R_1, \text{email}, \text{J@ed.ex})$
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?X	?Y
R_1	john
R_2	paul

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R_2	paul	

?X	?E
R_1	J@ed.ex

► from the **Union**

Boolean filter expressions (value constraints)

In filter expressions we consider:

- ▶ equality = among variables and RDF terms
- ▶ unary predicate **bound**
- ▶ boolean combinations (\wedge , \vee , \neg)

Satisfaction of value constraints

A mapping **satisfies**:

- ▶ $?X = c$ if it gives the value c to variable $?X$
- ▶ $?X = ?Y$ if it gives the same value to $?X$ and $?Y$
- ▶ $\text{bound}(?X)$ if it is defined for $?X$

Definition

Evaluation of $(P \text{ FILTER } R)$: Set of mappings in the evaluation of P that **satisfy** R .

The evaluation problem

Input:

A **mapping**, a graph **pattern**, and an RDF **graph**.

Question:

Is the **mapping** in the evaluation of the **pattern** against the **graph**?

Evaluation of simple patterns is polynomial

Theorem

For patterns using only AND and FILTER operators (AND-FILTER expressions), the evaluation problem is polynomial:

$O(\text{size of the pattern} \times \text{size of the graph})$.

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$$O(\text{size of the pattern} \times \text{size of the graph}).$$

Proof idea

- ▶ *Check that the mapping makes every triple to match.*
- ▶ *Then check that the mapping satisfies the FILTERs.*

Evaluation including UNION is NP-complete

Theorem

The evaluation problem is NP-complete for AND-FILTER-UNION expressions.

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The evaluation problem is NP-complete for AND-FILTER-UNION expressions.

Proof idea

- ▶ *Reduction from 3SAT.*
- ▶ \neg **bound** *is used to encode negation.*

In general: Evaluation problem is PSPACE-complete

Theorem

For general patterns that include OPT operator, the evaluation problem is PSPACE-complete.

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Can we efficiently evaluate SPARQL queries in practice?

In general: Evaluation problem is PSPACE-complete

Theorem

For general patterns that include OPT operator, the evaluation problem is PSPACE-complete.

Can we efficiently evaluate SPARQL queries in practice?

- ▶ We need to understand how the complexity depends on the operators of SPARQL.

A simple normal form

Proposition (UNION Normal Form)

Every graph pattern is equivalent to one of the form

$$P_1 \text{ UNION } P_2 \text{ UNION } \dots \text{ UNION } P_n$$

where each P_i is UNION-free.

A simple normal form

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Every graph pattern is equivalent to one of the form

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Graph pattern expressions are usually in this normal form.

A simple normal form

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where each P_i is UNION-free.

Graph pattern expressions are usually in this normal form.

Corollary

The evaluation problem is polynomial for AND-FILTER-UNION expressions in the UNION normal form.

PSPACE-completeness: A stronger lower bound

Theorem

*The evaluation problem remains PSPACE-complete for AND-FILTER-**OPT** expressions.*

PSPACE-completeness: A stronger lower bound

Theorem

The evaluation problem remains PSPACE-complete for AND-FILTER-OPT expressions.

Proof idea

- ▶ *Reduction from QBF: A pattern encodes a quantified propositional formula*

$$\forall x_1 \exists y_1 \forall x_2 \exists y_2 \cdots \psi.$$

PSPACE-completeness: A stronger lower bound

Theorem

*The evaluation problem remains PSPACE-complete for AND-FILTER-**OPT** expressions.*

Proof idea

- ▶ *Reduction from **QBF**: A pattern encodes a quantified propositional formula*

$$\forall x_1 \exists y_1 \forall x_2 \exists y_2 \cdots \psi.$$

- ▶ *Nested OPTs are used to encode quantifier alternation.*

PSPACE-hardness: A closer look

Assume $\varphi = \forall x_1 \exists y_1 \psi$, where $\psi = (x_1 \vee \neg y_1) \wedge (\neg x_1 \vee y_1)$.

We generate G , P_φ and μ_0 such that μ_0 belongs to the answer of P_φ over G iff φ is valid:

G :

R_ψ :

P_ψ :

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PSPACE-hardness: A closer look

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We generate G , P_φ and μ_0 such that μ_0 belongs to the answer of P_φ over G iff φ is valid:

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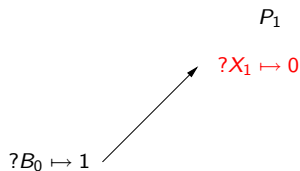
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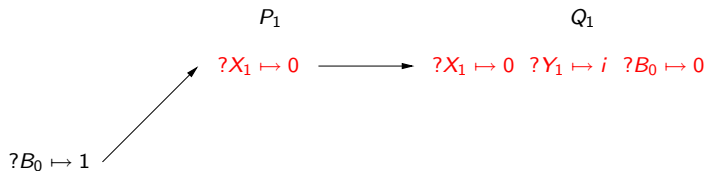
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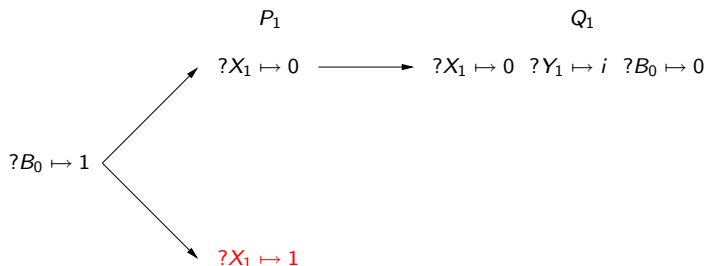
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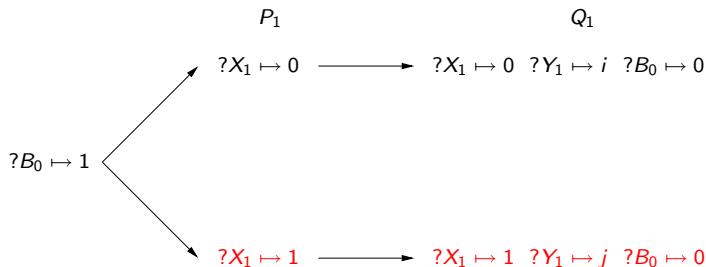
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AND-FILTER-OPT fragment: Reducing the complexity

Patterns in the reduction are not very natural:

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These patterns rarely occur in practice.

Well-designed patterns

Definition

An AND-FILTER-OPT pattern is well-designed if for every OPT in the pattern:

$$(\dots\dots\dots (A \text{ OPT } B) \dots\dots\dots)$$

if a variable occurs **inside B** and **anywhere outside the OPT operator**, then the variable **must also occur inside A** .

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Example

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*The evaluation problem is **coNP-complete** for well-designed AND-FILTER-OPT patterns.*

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The evaluation problem is coNP-complete for patterns of the form $P_1 \text{ UNION } P_2 \text{ UNION } \dots \text{ UNION } P_k$, where each P_i is a well-designed AND-FILTER-OPT pattern.

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Can we use this in practice?

- ▶ Well-designed patterns are suitable for optimization.

Classical optimization

- ▶ Classical optimization assumes **null-rejection**.
 - ▶ null-rejection: the join/outer-join condition must fail in the presence of nulls.
- ▶ SPARQL operations are **not null-rejecting**.
 - ▶ by definition of compatible mappings.

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Well-designed graph patterns and optimization

Consider the following rules:

$$((P_1 \text{ OPT } P_2) \text{ FILTER } R) \longrightarrow ((P_1 \text{ FILTER } R) \text{ OPT } P_2) \quad (1)$$

$$(P_1 \text{ AND } (P_2 \text{ OPT } P_3)) \longrightarrow ((P_1 \text{ AND } P_2) \text{ OPT } P_3) \quad (2)$$

$$((P_1 \text{ OPT } P_2) \text{ AND } P_3) \longrightarrow ((P_1 \text{ AND } P_3) \text{ OPT } P_2) \quad (3)$$

Proposition

If P is a well-designed pattern and Q is obtained from P by applying either (1) or (2) or (3), then Q is a well-designed pattern equivalent to P .

Well-designed graph patterns and optimization

A graph pattern P is in **OPT normal form** if there exist AND-FILTER patterns Q_1, \dots, Q_k such that:

P is constructed from Q_1, \dots, Q_k by using only the OPT operator.

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Patterns in OPT normal form can be evaluated more efficiently:

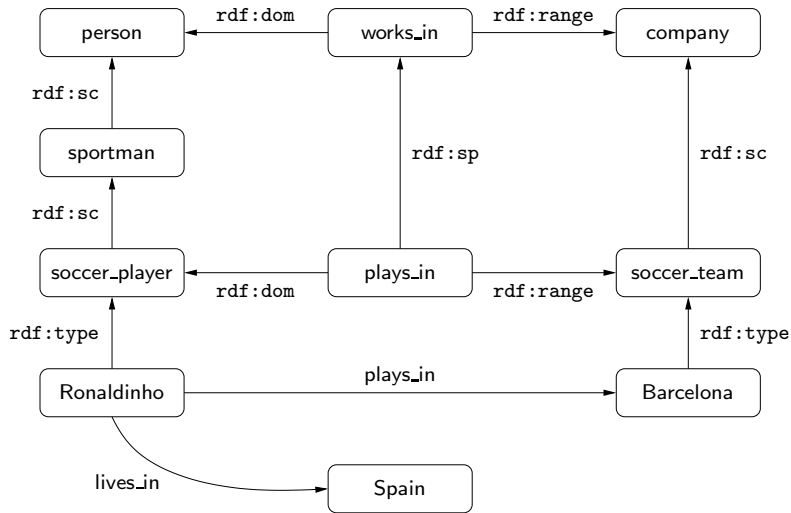
- ▶ AND-FILTER expressions are evaluated first, and then the results are combined using the OPT operator.

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Querying RDFS data

- ▶ RDFS extends RDF with a schema vocabulary: `subPropertyOf` (`rdf:sp`), `subClassOf` (`rdf:sc`), `domain` (`rdf:dom`), `range` (`rdf:range`), `type` (`rdf:type`).
- ▶ Evaluating queries which involve this vocabulary is challenging.
- ▶ There is not yet consensus in the Semantic Web community on how to define a query language for RDFS.

A simple SPARQL query: (Ronaldo, rdf:type, person)



SPARQL over RDFS

Checking whether a triple t is in a graph G is the basic step when answering queries over RDF.

- ▶ For the case of RDFS, we need to check whether t is implied by G .

The notion of entailment in RDFS can be defined in terms of classical notions such model, interpretation, etc.

- ▶ As for the case of first-order logic.

This notion can also be characterized by a set of [inference rules](#).

Entailment in RDFS

There are inference systems characterizing the notion of entailment in RDFS:

Subproperty rules : $\frac{(p, \text{rdf:sp}, q) \quad (a, p, b)}{(a, q, b)}$

Subclass rules : $\frac{(a, \text{rdf:sc}, b) \quad (b, \text{rdf:sc}, c)}{(a, \text{rdf:sc}, c)}$

Typing rules : $\frac{(p, \text{rdf:dom}, c) \quad (a, p, b)}{(a, \text{rdf:type}, c)}$

...

SPARQL over RDFS: Closure of a graph

The closure of an RDFS graph G , denoted by $cl(G)$, is the graph obtained by adding to G all the triples that are implied by G .

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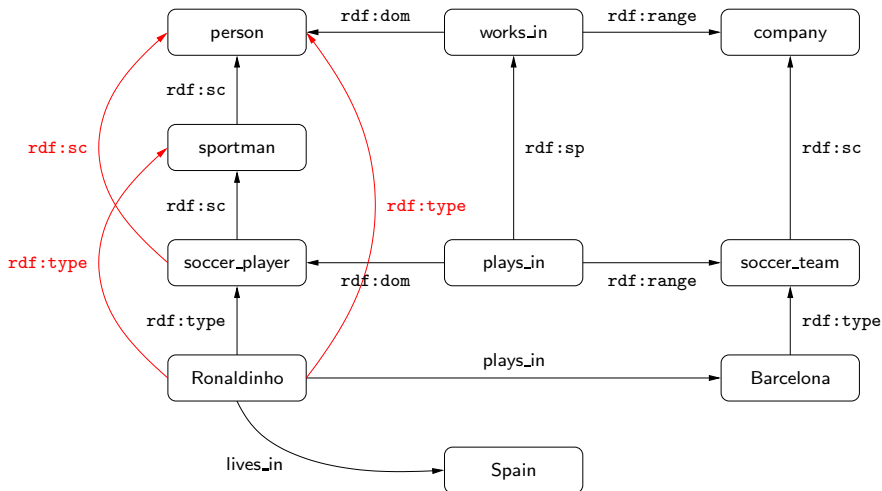
Basic step for answering queries over RDFS:

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Definition

The *RDFS-evaluation* of a graph pattern P over an RDFS graph G is defined as the evaluation of P over $\text{cl}(G)$.

Example: (Ronaldo, rdf:type, person) over the closure



Answering SPARQL queries over RDFS

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- ▶ The size of the closure of G can be quadratic in the size of G .
- ▶ Once the closure has been computed, all the queries are evaluated over a graph which can be much larger than the original graph.
- ▶ The approach is not goal-oriented.

When evaluating $(a, \text{rdf:sc}, b)$, a goal-oriented approach should not compute $\text{cl}(G)$:

- ▶ It should just verify whether there exists a path from a to b in G where every edge has label rdf:sc .

Extending SPARQL with navigational capabilities

The example $(a, \text{rdf:sc}, b)$ suggests that a query language with navigational capabilities could be appropriate for RDFS.

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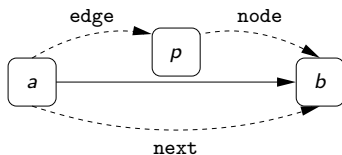
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- ▶ It is goal-oriented.
- ▶ It has been used to design query languages for XML (e.g., XPath and XQuery). The results for these languages can be used here.
- ▶ Navigational operators allow to express natural queries that are **not expressible in SPARQL over RDFS**.

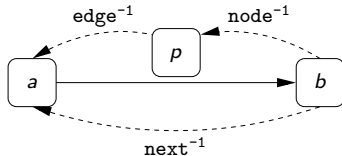
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Navigational axes

Forward axes for an RDF triple (a, p, b) :



Backward axes for an RDF triple (a, p, b) :



A first attempt: 0-NAV-SPARQL

Syntax of navigational expressions:

$$\text{exp} := \text{self} \mid \text{self}::a \mid \text{axis} \mid \\ \text{axis}::a \mid \text{exp}/\text{exp} \mid \text{exp}|\text{exp} \mid \text{exp}^*$$

where $a \in U$ and $\text{axis} \in \{\text{next}, \text{next}^{-1}, \text{edge}, \text{edge}^{-1}, \text{node}, \text{node}^{-1}\}$.

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Syntax of 0-NAV-SPARQL: SPARQL extended with triples of the form (x, exp, y) , where exp is a navigational expression.

- ▶ Examples: (Ronaldo, `next::lives_in`, Spain) and $(?X, (\text{next}::(\text{rdf}:\text{sc}))^+, ?Y)$.

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Example: $(?X, (\text{next}::\text{Iberia})^+, ?Y)$ AND $(?X, (\text{next}::\text{AirFrance})^+, ?Y)$

Is 0-NAV-SPARQL a good language for RDFS?

How do we test whether a language is appropriate for RDFS?

- ▶ Can we capture SPARQL over RDFS?

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For every RDFS graph G and SPARQL pattern P , we would like to find a 0-NAV-SPARQL pattern Q such that:

- ▶ RDFS-evaluation of P over G = evaluation of Q over G .

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There is a SPARQL pattern P for which there is no 0-NAV-SPARQL pattern Q such that, for every RDFS graph G :

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- ▶ We adopt the notion of branching from XPath.

A successful attempt: NAV-SPARQL

Syntax of navigational expressions:

$$\begin{aligned} \text{exp} &:= \text{self} \mid \text{self}::a \mid \text{axis} \mid \\ &\quad \text{axis}::a \mid \text{axis}::[\text{exp}] \mid \text{exp}/\text{exp} \mid \text{exp}|\text{exp} \mid \text{exp}^* \end{aligned}$$

where $a \in U$ and $\text{axis} \in \{\text{next}, \text{next}^{-1}, \text{edge}, \text{edge}^{-1}, \text{node}, \text{node}^{-1}\}$.

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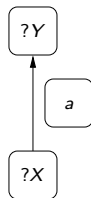
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NAV-SPARQL: Capturing SPARQL over RDFS

Example: $(?X, a, ?Y)$ over RDFS is equivalent to NAV-SPARQL pattern $(?X, \text{next}::[(\text{next}::(\text{rdf}:\text{sp}))^*/(\text{self}::a)], ?Y)$.

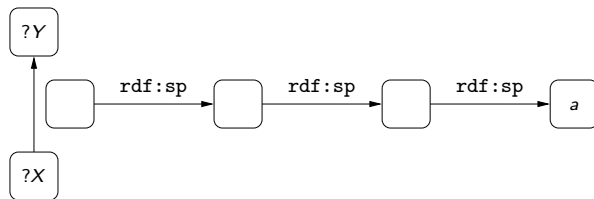
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Proof idea

Replace $(?X, a, ?Y)$ by $(?X, R(a), ?Y)$, where:

$$R(\text{rdf:sc}) = (\text{next::}(\text{rdf:sc}))^+$$

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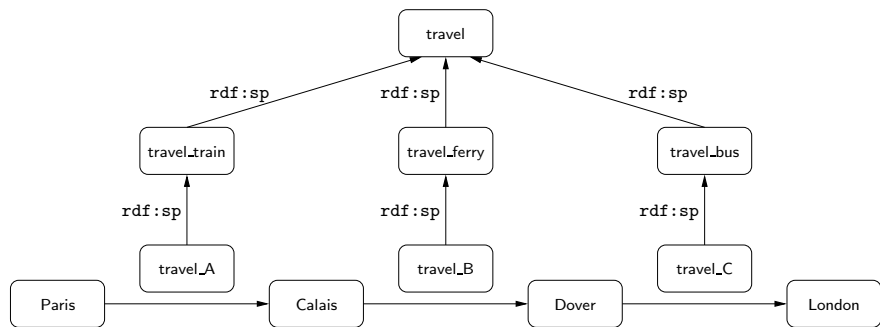
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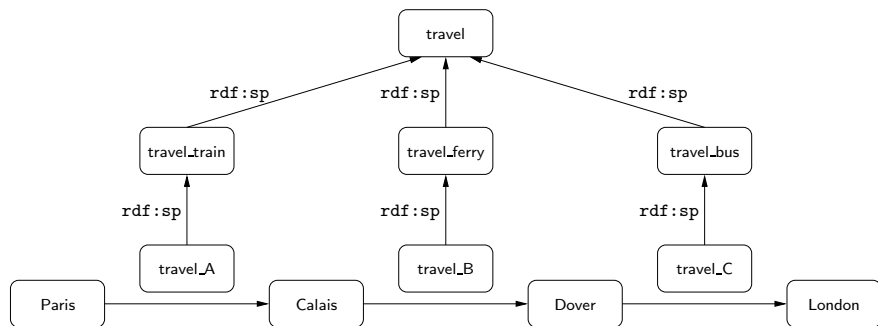
$$R(b) = \text{next::}[(\text{next::}(\text{rdf:sp}))^*/(\text{self::}b)]$$

Note: $R(\text{rdf:type})$ uses next, edge and node⁻¹.

The extra expressive power of NAV-SPARQL

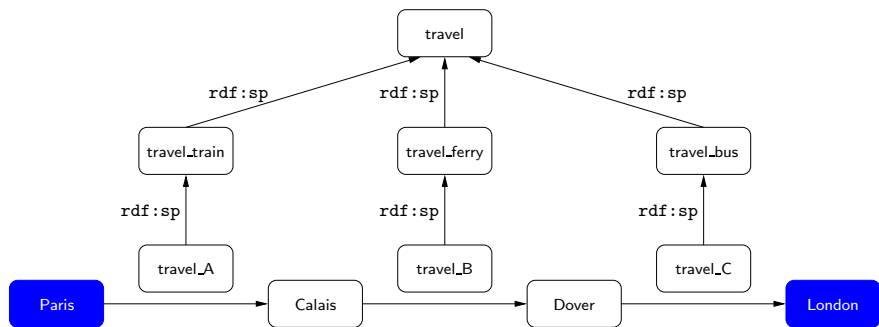


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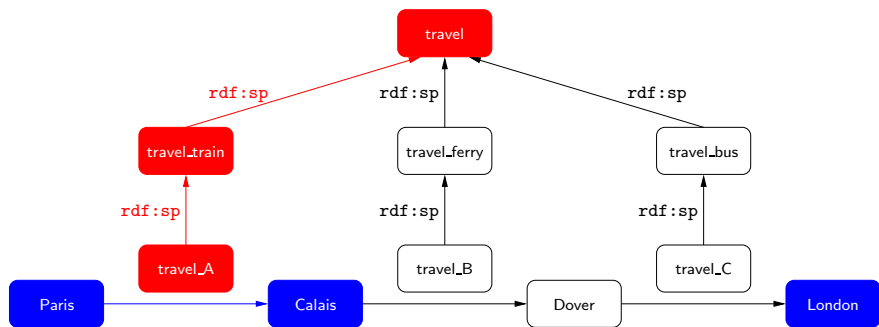
A natural query: $(?X, (\text{next}::[(\text{next}::(\text{rdf:sp}))^*/(\text{self}::\text{travel})])^+, ?Y)$

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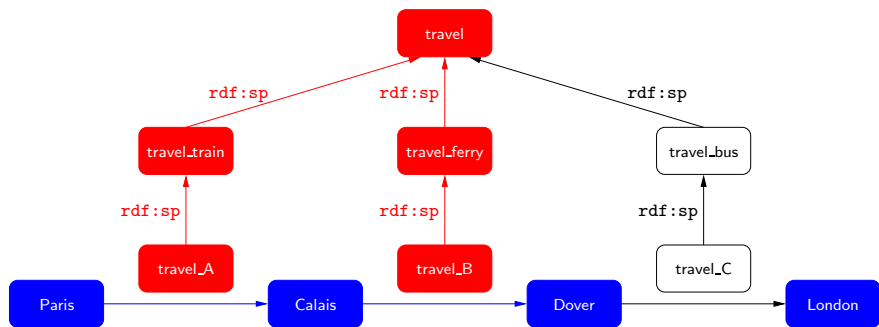
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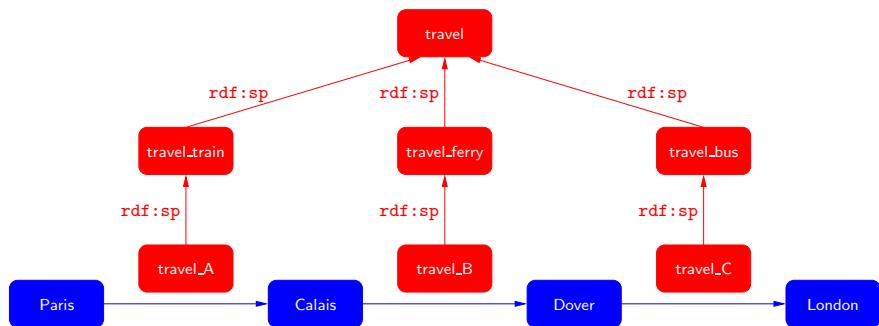
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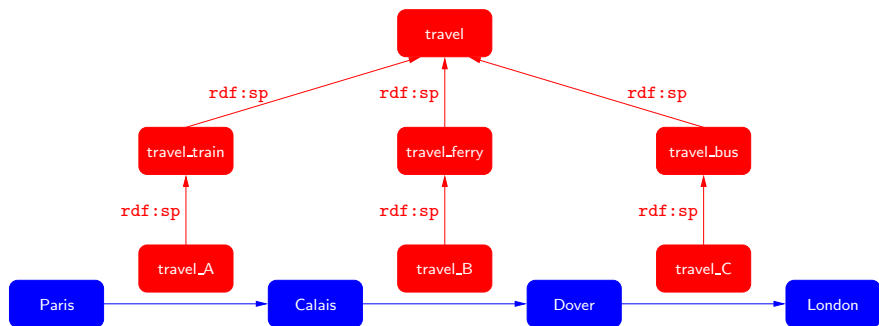
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- ▶ This query cannot be expressed in SPARQL over RDFS.

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- ▶ Implementation of SPARQL.

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 - ▶ Is there a fragment of NAV-SPARQL which is also appropriate for RDFS? One level of nesting is enough to capture SPARQL over RDFS.