

Exchanging more than Complete Data

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Joint work with Jorge Pérez (U. de Chile) and Juan Reutter (U. Edinburgh)

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- The data exchange problem
 - Some fundamental results in relational data exchange
- The need for a more general data exchange framework
 - Two important scenarios: Incomplete databases (open-world databases: RDF) and knowledge bases

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▶ The data exchange problem

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Given: A source schema ${\bf S},$ a target schema ${\bf T}$ and a specification Σ of the relationship between these schemas

Data exchange: Problem of materializing an instance of ${\bf T}$ given an instance of ${\bf S}$

- Target instance should reflect the source data as accurately as possible, given the constraints imposed by Σ and T
- It should be efficiently computable
- It should allow one to evaluate queries on the target in a way that is *semantically consistent* with the source data

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Schema T

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What are the challenges in the area?

- What is a good language for specifying the relationship between source and target data?
 - Expressiveness versus complexity
- What is a good instance to materialize?
- What does it mean to answer a query over target data?
- How do we answer queries over target data? Can we do this efficiently?

Exchanging relational data

The data exchange problem has been extensively studied in the relational world.

It has also been commercially implemented: IBM Clio

Relational data exchange setting:

- Source and target schemas: Relational schemas
- Relationship between source and target schemas: Source-to-target tuple-generating dependencies (st-tgds)

Semantics of data exchange has been precisely defined.

 Efficient algorithms for materializing target instances and for answering queries over the target schema have been developed

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Schema mapping: The key component in relational data exchange

Schema mapping: $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$

- **S** and **T** are disjoint relational schemas
- Σ is a finite set of st-tgds:

 $\forall \bar{x} \forall \bar{y} \left(\varphi(\bar{x}, \bar{y}) \to \exists \bar{z} \, \psi(\bar{x}, \bar{z}) \right)$

 $\varphi(\bar{x}, \bar{y})$: conjunction of relational atomic formulas over **S** $\psi(\bar{x}, \bar{z})$: conjunction of relational atomic formulas over **T**

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Relational schema mappings: An example



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Relational schema mappings: An example



Note

We omit universal quantifiers in st-tgds:

$$\texttt{Employee}(x) \rightarrow \exists y \texttt{Dept}(x, y)$$

Relational data exchange problem

Fixed: $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$

Problem: Given instance *I* of **S**, find an instance *J* of **T** such that (I, J) satisfies Σ

▶ (I, J) satisfies $\varphi(\bar{x}, \bar{y}) \rightarrow \exists \bar{z} \psi(\bar{x}, \bar{z})$ if whenever I satisfies $\varphi(\bar{a}, \bar{b})$, there is a tuple \bar{c} such that J satisfies $\psi(\bar{a}, \bar{c})$

Relational data exchange problem

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Notation

- J is a solution for I under \mathcal{M}
 - ▶ $Sol_{\mathcal{M}}(I)$: Set of solutions for I under \mathcal{M}

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Example

- S: Employee(name)
- T: Dept(name, number)
- Σ : Employee $(x) \rightarrow \exists y \operatorname{Dept}(x, y)$

Solutions for $I = \{\text{Employee}(\text{Peter})\}$:

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Example

- S: Employee(name)
- T: Dept(name, number)
- Σ : Employee $(x) \rightarrow \exists y \operatorname{Dept}(x, y)$

```
Solutions for I = {Employee(Peter)}:
```

```
J_1: \{ \texttt{Dept}(\texttt{Peter}, 1) \}
```

Example

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Solutions for $I = \{\text{Employee}(\text{Peter})\}$:

```
J_1: {Dept(Peter, 1)}
```

J₂: {Dept(Peter,1), Dept(Peter,2)}

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Example

- S: Employee(name)
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- Σ : Employee(x) $\rightarrow \exists y \operatorname{Dept}(x, y)$

Solutions for $I = \{\text{Employee}(\text{Peter})\}$:

- $J_1: {Dept(Peter, 1)}$
- J₂: {Dept(Peter,1), Dept(Peter,2)}
- J_3 : {Dept(Peter,1), Dept(John,1)}

Example

- S: Employee(name)
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Solutions for $I = \{\text{Employee}(\text{Peter})\}$:

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- J₂: {Dept(Peter,1), Dept(Peter,2)}
- J_3 : {Dept(Peter,1), Dept(John,1)}
- $J_4: \{ \text{Dept}(\text{Peter}, n_1) \}$

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Example

- S: Employee(name)
- T: Dept(name, number)
- Σ : Employee $(x) \rightarrow \exists y \operatorname{Dept}(x, y)$

Solutions for $I = \{\text{Employee}(\text{Peter})\}$:

- $J_1: \{ \texttt{Dept}(\texttt{Peter}, 1) \}$
- J₂: {Dept(Peter,1), Dept(Peter,2)}
- J_3 : {Dept(Peter,1), Dept(John,1)}
- $J_4: \{ \text{Dept}(\text{Peter}, \frac{n_1}{n_1}) \}$
- $J_5: \{ \text{Dept}(\text{Peter}, n_1), \text{Dept}(\text{Peter}, n_2) \}$

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Algorithm (Chase)

- Input : $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$ and an instance I of \mathbf{S}
- Output : Canonical universal solution J^* for I under \mathcal{M}

```
let J^* := \text{empty instance of } \mathbf{T}
for every \varphi(\bar{x}, \bar{y}) \to \exists \bar{z} \, \psi(\bar{x}, \bar{z}) \text{ in } \Sigma \text{ do}
for every \bar{a}, \bar{b} such that I satisfies \varphi(\bar{a}, \bar{b}) do
create a fresh tuple \bar{n} of pairwise distinct null values
insert \psi(\bar{a}, \bar{n}) into J^*
```

Canonical universal solution: Example

Example

Consider mapping \mathcal{M} specified by dependency:

```
\texttt{Employee}(x) \rightarrow \exists y \texttt{Dept}(x, y)
```

Canonical universal solution for

I = {Employee(Peter), Employee(John)}:

▶ For a = Peter do

- Create a fresh null value n_1
- Insert Dept(Peter, n₁) into J*

For a = John do

- Create a fresh null value n2
- ► Insert Dept(John, n₂) into J^{*}

Result: $J^* = \{ \text{Dept}(\text{Peter}, n_1), \text{Dept}(\text{John}, n_2) \}$

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Given: Mapping \mathcal{M} , source instance I and query Q over the target schema

▶ What does it mean to answer Q?

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ExampleConsider mapping \mathcal{M} specified by:
 $\operatorname{Employee}(x) \rightarrow \exists y \operatorname{Dept}(x, y)$ Given instance $I = \{\operatorname{Employee}(\operatorname{Peter})\}:$
 $\operatorname{certain}_{\mathcal{M}}(\exists y \operatorname{Dept}(x, y), I) = \{\operatorname{Peter}\}$
 $\operatorname{certain}_{\mathcal{M}}(\operatorname{Dept}(x, y), I) = \emptyset$

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Query rewriting: An approach for answering queries

How can we compute certain answers?

Naïve algorithm does not work: infinitely many solutions

How can we compute certain answers?

Naïve algorithm does not work: infinitely many solutions

Approach proposed in [FKMP03]: Query Rewriting

Given a mapping \mathcal{M} and a target query Q, compute a query Q^* such that for every source instance I with canonical universal solution J^* :

$$\operatorname{certain}_{\mathcal{M}}(Q,I) = Q^{\star}(J^{\star})$$

Query rewriting over the canonical universal solution

Theorem (FKMP03)

Given a mapping \mathcal{M} specified by st-tgds and a union of conjunctive queries Q, there exists a query Q^* such that for every source instance I with canonical universal solution J^* :

 $\operatorname{certain}_{\mathcal{M}}(Q, I) = Q^{\star}(J^{\star})$

Query rewriting over the canonical universal solution

Theorem (FKMP03)

Given a mapping \mathcal{M} specified by st-tgds and a union of conjunctive queries Q, there exists a query Q^* such that for every source instance I with canonical universal solution J^* :

$$\operatorname{certain}_{\mathcal{M}}(Q, I) = Q^{\star}(J^{\star})$$

Proof idea: Assume that C(a) holds whenever *a* is a constant.

Then:

$$Q^{\star}(x_1,\ldots,x_m) = \mathbf{C}(x_1) \wedge \cdots \wedge \mathbf{C}(x_m) \wedge Q(x_1,\ldots,x_m)$$

Data complexity: Data exchange setting and query are considered to be fixed.

Corollary (FKMP03)

For mappings given by st-tgds, certain answers for **UCQ** can be computed in polynomial time (data complexity)

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Relational data exchange: Some lessons learned

Key steps in the development of the area:

- ► Definition of schema mappings: Precise syntax and semantics
 - Definition of the notion of solution
- Identification of good solutions
- Polynomial time algorithms for materializing good solutions
- Definition of target queries: Precise semantics
- Polynomial time algorithms for computing certain answers for UCQ

Relational data exchange: Some lessons learned

Key steps in the development of the area:

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Creating schema mappings is a time consuming and expensive process

Manual or semi-automatic process in general

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Ongoing project: Reusing schema mappings






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We need some operators for schema mappings



We need some operators for schema mappings

Composition in the above case

Contributions mentioned in the previous slides are just a first step towards the development of a general framework for data exchange.

In fact, as pointed in [B03],

many information system problems involve not only the design and integration of complex application artifacts, but also their subsequent manipulation. This has motivated the need for the development of a general infrastructure for managing schema mappings.

The problem of managing schema mappings is called **metadata management**.

High-level algebraic operators, such as compose, are used to manipulate mappings.

What other operators are needed?

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Composition and inverse operators have to be combined



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Composition and inverse operators have been extensively studied in the relational world.

Semantics, computation, ...

Combining these operators is an open issue.

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 Key observation: A target instance of a mapping can be the source instance of another mapping

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- Key observation: A target instance of a mapping can be the source instance of another mapping
- Sources instances may contain null values

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Semantics, computation, ...

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- Key observation: A target instance of a mapping can be the source instance of another mapping
- Sources instances may contain null values

There is a need for a data exchange framework that can handle databases with incomplete information.

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There is an increasing interest in publishing relational data as RDF

Resulted in the creation of the W3C RDB2RDF Working Group

The problem of translating relational data into RDF can be seen as a data exchange problem

 Schema mappings can be used to describe how the relational data is to be mapped into RDF

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The problem of translating relational data into RDF can be seen as a data exchange problem

 Schema mappings can be used to describe how the relational data is to be mapped into RDF

But there is a mismatch here: A relational database under a closed-world semantics is to be translated into an RDF graph under an open-world semantics

There is a need for a data exchange framework that can handle both databases with complete and incomplete information

An issue discussed at the W3C RDB2RDF Working Group: Is a mapping information preserving?

▶ In particular: For the default mapping defined by this group

How can we address this issue?

Metadata management can help us

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Question to answer: Is a mapping invertible?

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How can we address this issue?

Metadata management can help us

Question to answer: Is a mapping invertible?

- This time an RDF graph is to be translated into a relational database!
- ▶ We want to have a unifying framework for all these cases

But these are not the only reasons ...

Nowadays several applications use knowledge bases to represent data.

- A knowledge base has not only data but also rules that allows to infer new data
- In the Semantics Web: RDFS and OWL ontologies

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- A knowledge base has not only data but also rules that allows to infer new data
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In a data exchange application over the Semantics Web:

The input is a mapping and a source specification including data and rules, and the output is a target specification also including data and rules

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There is a need for a data exchange framework that can handle knowledge bases.

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Example

Assume given the following source knowledge base:

Data:

Rules:

Fa	ather		Mother	
Andy	Bob		Carrie Bob	
Bob	Danny			
Danny	/ Eddie			
	()		- ()	
	Father(x, y)	\rightarrow	Parent(x, y)	
	Mother(x, y)	\rightarrow	Parent(x, y)	
Parent(x, y)	$\wedge \texttt{Parent}(y, z)$	\rightarrow	Grandparent(x, z))

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Example (cont'd)

Given a mapping:

$$Father(x, y) \rightarrow F(x, y)$$

Grandparent $(x, y) \rightarrow G(x, y)$

What is a good translation of the initial knowledge base?

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Example (cont'd)

Given a mapping:

$$\operatorname{Father}(x,y) \rightarrow \operatorname{F}(x,y)$$

 $\operatorname{Grandparent}(x,y) \rightarrow \operatorname{G}(x,y)$

What is a good translation of the initial knowledge base?

Data:



Example (cont'd)

Our first alternative does not include any translation of the source rules:

$$Father(x, y) \rightarrow Parent(x, y)$$

 $Mother(x, y) \rightarrow Parent(x, y)$
 $ent(x, y) \wedge Parent(y, z) \rightarrow Grandparent(x, z)$

$$Parent(x, y) \land Parent(y, z) \rightarrow Grandparent(x, y)$$

Example (cont'd)

Our first alternative does not include any translation of the source rules:

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Example (cont'd)

Our first alternative does not include any translation of the source rules:

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What data should we materialize?

Example (cont'd)

Our first alternative does not include any translation of the source rules:

$$\mathbf{F}(x,y) \wedge \mathbf{F}(y,z) \quad \rightarrow \quad \mathbf{G}(x,z)$$

What data should we materialize?

I	7		G	
Andy	Bob	/	Andy	Danny
Bob	Danny	(Carrie	Danny
Danny	Eddie	I	Bob	Eddie

Example (cont'd)

Our first alternative does not include any translation of the source rules:

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Example (cont'd)

Our first alternative does not include any translation of the source rules:

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G

Danny

Carrie

What data should we materialize?

I	7
Andy	Bob
Bob	Danny
Danny	Eddie

Is this a good translation? Why?
One can exchange more than complete data

- In data exchange one starts with a database instance (with complete information).
- What if we have an initial object that has several interpretations?
 - A representation of a set of possible instances
- We propose a new general formalism to exchange representations of possible instances
 - We apply it to the problems of exchanging instances with incomplete information and exchanging knowledge bases

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- Formalism for exchanging representations systems
- Applications to incomplete instances
- Applications to knowledge bases
- Concluding remarks

- Formalism for exchanging representations systems
- Applications to incomplete instances
- Applications to knowledge bases
- Concluding remarks

Representation systems

A representation system $\mathcal{R} = (\mathbf{W}, rep)$ consists of:

- ► a set W of *representatives*
- a function rep that assigns a set of instances to every element in W

$$\mathsf{rep}(\mathcal{V}) = \{\mathit{I}_1, \mathit{I}_2, \mathit{I}_3, \ldots\}$$
 for every $\mathcal{V} \in \mathbf{W}$

Uniformity assumption: For every $\mathcal{V} \in \mathbf{W}$, there exists a relational schema **S** (the type of \mathcal{V}) such that $rep(\mathcal{V}) \subseteq Inst(\mathbf{S})$

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Incomplete instances and knowledge bases are representation systems

In classical data exchange we consider only complete data

Recall that given $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$, $I \in \text{Inst}(\mathbf{S})$ and $J \in \text{Inst}(\mathbf{T})$: J is a solution for I under \mathcal{M} if $(I, J) \models \Sigma$

 $J \in \mathsf{Sol}_{\mathcal{M}}(I)$

In classical data exchange we consider only complete data

Recall that given $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$, $I \in \text{Inst}(\mathbf{S})$ and $J \in \text{Inst}(\mathbf{T})$: J is a solution for I under \mathcal{M} if $(I, J) \models \Sigma$

 $J \in \mathsf{Sol}_\mathcal{M}(I)$

This can be extended to set of instances. Given $\mathcal{X} \subseteq \text{Inst}(\mathbf{S})$:

$$\mathsf{Sol}_\mathcal{M}(\mathcal{X}) \;\;=\;\; igcup_{I\in\mathcal{X}}\mathsf{Sol}_\mathcal{M}(I)$$

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Extending the definition to representation systems

Given:

- ► a mapping $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$
- a representation system $\mathcal{R} = (\mathbf{W}, \mathsf{rep})$
- ▶ $\mathcal{U}, \mathcal{V} \in \mathbf{W}$ of types **S** and **T**, respectively

Extending the definition to representation systems

Given:

- ► a mapping $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$
- a representation system $\mathcal{R} = (\mathbf{W}, \mathsf{rep})$
- $\blacktriangleright~ \mathcal{U}, \mathcal{V} \in \textbf{W}$ of types S and T, respectively

Definition (APR11)

 ${\mathcal V}$ is an ${\mathcal R}\text{-}{\it solution}$ of ${\mathcal U}$ under ${\mathcal M}$ if

 $\mathsf{rep}(\mathcal{V}) \subseteq \mathsf{Sol}_{\mathcal{M}}(\mathsf{rep}(\mathcal{U}))$

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Extending the definition to representation systems

Given:

- ► a mapping $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$
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Definition (APR11)

 ${\mathcal V}$ is an ${\mathcal R}\mbox{-}{\it solution}$ of ${\mathcal U}$ under ${\mathcal M}$ if

 $\mathsf{rep}(\mathcal{V}) \ \subseteq \ \mathsf{Sol}_{\mathcal{M}}(\mathsf{rep}(\mathcal{U}))$

Or equivalently: \mathcal{V} is an \mathcal{R} -solution of \mathcal{U} if for every $J \in \operatorname{rep}(\mathcal{V})$, there exists $I \in \operatorname{rep}(\mathcal{U})$ such that $J \in \operatorname{Sol}_{\mathcal{M}}(I)$.

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What is a good solution in this framework?

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What is a good solution in this framework?

Definition (APR11)

 ${\mathcal V}$ is an universal ${\mathcal R}\text{-solution}$ of ${\mathcal U}$ under ${\mathcal M}$ if

 $\operatorname{rep}(\mathcal{V}) = \operatorname{Sol}_{\mathcal{M}}(\operatorname{rep}(\mathcal{U}))$

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Let C be a class of mappings.

Let \mathcal{C} be a class of mappings.

 $\operatorname{rep}(\mathcal{V}) = \operatorname{Sol}_{\mathcal{M}}(\operatorname{rep}(\mathcal{U}))$

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Let \mathcal{C} be a class of mappings.

Definition (APR11)

 $\begin{aligned} \mathcal{R} &= (\mathbf{W}, \mathsf{rep}) \text{ is a strong representation system for } \mathcal{C} \text{ if for every} \\ \mathcal{M} \in \mathcal{C} \text{ from } \mathbf{S} \text{ to } \mathbf{T}, \text{ and for every } \mathcal{U} \in \mathbf{W} \\ \mathcal{V} \in \mathbf{W} \end{aligned}$, there exists a $\mathcal{V} \in \mathbf{W}$

 $\operatorname{rep}(\mathcal{V}) = \operatorname{Sol}_{\mathcal{M}}(\operatorname{rep}(\mathcal{U}))$

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Let \mathcal{C} be a class of mappings.

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 $\operatorname{rep}(\mathcal{V}) = \operatorname{Sol}_{\mathcal{M}}(\operatorname{rep}(\mathcal{U}))$

Let \mathcal{C} be a class of mappings.

Definition (APR11)

 $\mathcal{R} = (\mathbf{W}, \text{rep})$ is a *strong representation system* for \mathcal{C} if for every $\mathcal{M} \in \mathcal{C}$ from **S** to **T**, and for every $\mathcal{U} \in \mathbf{W}$ of type **S**, there exists a $\mathcal{V} \in \mathbf{W}$ of type **T**:

 $\operatorname{rep}(\mathcal{V}) = \operatorname{Sol}_{\mathcal{M}}(\operatorname{rep}(\mathcal{U}))$

Let \mathcal{C} be a class of mappings.

Definition (APR11)

 $\mathcal{R} = (\mathbf{W}, \text{rep})$ is a *strong representation system* for \mathcal{C} if for every $\mathcal{M} \in \mathcal{C}$ from **S** to **T**, and for every $\mathcal{U} \in \mathbf{W}$ of type **S**, there exists a $\mathcal{V} \in \mathbf{W}$ of type **T**:

 $\operatorname{rep}(\mathcal{V}) = \operatorname{Sol}_{\mathcal{M}}(\operatorname{rep}(\mathcal{U}))$

If $\mathcal{R} = (\mathbf{W}, \text{rep})$ is a strong representation system, then the universal solutions for the representatives in \mathbf{W} can be represented in the same system.

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- Formalism for exchanging representations systems
- Applications to incomplete instances
- Applications to knowledge bases
- Concluding remarks

What is a strong representation system for the class of mappings specified by st-tgds?

Are instances including nulls enough?

Can the fundamental data exchange problems be solved in polynomial time in this setting?

- Computing (universal) solutions
- Computing certain answers

Naive instances

We have already considered naive instances: Instances with null values

Example: Canonical universal solution

A naive instance ${\mathcal I}$ has labeled nulls:

 $R(1, n_1)$ $R(n_1, 2)$ $R(1, n_2)$

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Naive instances

We have already considered naive instances: Instances with null values

Example: Canonical universal solution

A naive instance ${\mathcal I}$ has labeled nulls:

$$R(1, n_1)$$

 $R(n_1, 2)$
 $R(1, n_2)$

The interpretations of ${\mathcal I}$ are constructed by replacing nulls by constants:

 $\operatorname{rep}(\mathcal{I}) = \{K \mid \mu(\mathcal{I}) \subseteq K \text{ for some valuation } \mu\}$

Naive instances have been extensively used in data exchange:

Proposition (FKMP03)

Let $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$, where Σ is a set of st-tgds. Then for every instance I of \mathbf{S} , there exists a naive instance \mathcal{J} of \mathbf{T} such that:

 $rep(\mathcal{J}) = Sol_{\mathcal{M}}(I)$

In fact, the canonical universal solution satisfies the property mentioned above.

But naive instances are not expressive enough to deal with incomplete information in the source instances:

Proposition (APR11)

Naive instances are not a strong representation system for the class of mappings specified by st-tgds

Are naive instances expressive enough?

Example

Consider a mapping ${\mathcal M}$ specified by:

 $Manager(x, y) \rightarrow Reports(x, y)$ $Manager(x, x) \rightarrow SelfManager(x)$

The canonical universal solution for $\mathcal{I} = \{\text{Manager}(n, \text{Peter})\}$ under \mathcal{M} : $\mathcal{J} = \{\text{Reports}(n, \text{Peter})\}$

But \mathcal{J} is not a *good* solution for \mathcal{I} .

It cannot represent the fact that if n is given value Peter, then SelfManager(Peter) should hold in the target.

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What should be added to naive instances to obtain a strong representation system?

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What should be added to naive instances to obtain a strong representation system?

Answer from database theory: Conditions on the nulls

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What should be added to naive instances to obtain a strong representation system?

Answer from database theory: Conditions on the nulls

Conditional instances: Naive instances plus tuple conditions

- A tuple condition is a positive Boolean combinations of:
 - equalities and inequalities between nulls, and between nulls and constants

Example

$$\begin{array}{c|c} R(1, n_1) & n_1 = n_2 \\ R(n_1, n_2) & n_1 \neq n_2 \ \lor \ n_2 = 2 \end{array}$$

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Example

Semantics:

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Example

Semantics:

$$\mu(n_1) = \mu(n_2) = 2 \qquad \mu(n_1) = \mu(n_2) = 3 \qquad \mu(n_1) = 2, \mu(n_2) = 3$$

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Example

Semantics:

$$\frac{\mu(n_1) = \mu(n_2) = 2}{R(1,2)} \qquad \frac{\mu(n_1) = \mu(n_2) = 3}{R(2,2)} \qquad \frac{\mu(n_1) = 2, \mu(n_2) = 3}{\mu(n_1) = 2, \mu(n_2) = 3}$$

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Example

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Example

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Interpretations of a conditional instance \mathcal{I} :

$$\mathsf{rep}(\mathcal{I}) = \{ \mathsf{K} \mid \mu(\mathcal{I}) \subseteq \mathsf{K} \text{ for some valuation } \mu \}$$

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Many problems are intractable over conditional instances.

▶ We also consider a restricted class of conditional instances

Positive conditional instances: Conditional instances without inequalities
(Positive) conditional instances are enough

Theorem (APR11)

Both conditional instances and positive conditional instances are strong representation systems for the class of mappings specified by st-tgds.

Example Consider again the mapping \mathcal{M} specified by: $Manager(x, y) \rightarrow Reports(x, y)$ $Manager(x, x) \rightarrow SelfManager(x)$ The following is a universal solution for $\mathcal{I} = \{\text{Manager}(n, \text{Peter})\}$ Reports(n, Peter) true SelfManager(Peter) n = Peter

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Positive conditional instances are *exactly* the needed representation system

Positive conditional instances are minimal:

Theorem (APR11)

All the following are needed to obtain a strong representation system for the class of mappings specified by st-tgds:

- equalities between nulls
- equalities between constant and nulls
- conjunctions and disjunctions

Conditional instances are enough but not minimal.

Positive conditional instance can be used in practice!

Let $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$, where Σ is a set of st-tgds.

Positive conditional instance can be used in practice!

Let $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$, where Σ is a set of st-tgds.

Theorem (APR11)

There exists a polynomial time algorithm that, given a positive conditional instance \mathcal{I} over **S**, computes a positive conditional instance \mathcal{J} over **T** that is a universal solution for \mathcal{I} under \mathcal{M} .

Positive conditional instance can be used in practice!

Let $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$, where Σ is a set of st-tgds.

Theorem (APR11)

There exists a polynomial time algorithm that, given a positive conditional instance \mathcal{I} over **S**, computes a positive conditional instance \mathcal{J} over **T** that is a universal solution for \mathcal{I} under \mathcal{M} .

Let Q be a union of conjunctive queries over **T**.

$$\begin{array}{lll} Q(\mathcal{J}) & = & \bigcap_{J \in \mathsf{rep}(\mathcal{J})} Q(J) \\ \mathsf{certain}_{\mathcal{M}}(Q, \mathcal{I}) & = & \bigcap_{\mathcal{J} \text{ is a solution for } \mathcal{I} \text{ under } \mathcal{M}} Q(\mathcal{J}) \end{array}$$

Theorem (APR11)

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The same result holds for the class of unions of conjunctive queries with at most one inequality per disjunct.

The other important class of queries in the data exchange area for which certain answers can be computed in polynomial time

- Formalism for exchanging representations systems
- Applications to incomplete instances
- Applications to knowledge bases
- Concluding remarks

The semantics of *knowledge bases* is given by sets of instances

Knowledge base over **S**: (I, Γ) such that

- ► *I* ∈ Inst(**S**)
- Γ a set of rules over S

Semantics: finite models

 $Mod(I,\Gamma) = \{K \in Inst(\mathbf{S}) \mid I \subseteq K \text{ and } K \models \Gamma\}$

We can apply our formalism to knowledge bases

 (I_2, Γ_2) is a KB-solution for (I_1, Γ_1) under $\mathcal M$ if:

 $Mod(I_2,\Gamma_2) \subseteq Sol_{\mathcal{M}}(Mod(I_1,\Gamma_1))$

 (I_2, Γ_2) is a *universal KB-solution* for (I_1, Γ_1) under \mathcal{M} if:

 $Mod(I_2, \Gamma_2) = Sol_{\mathcal{M}}(Mod(I_1, \Gamma_1))$

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Same as for the case of instances with incomplete information.

- Constructing universal KB-solutions
- Answering target queries

New fundamental problem: Construct solutions including as much implicit knowledge as possible.

What are good knowledge-base solutions?

First alternative: universal KB-solutions

But there exist some other KB-solutions desirable to materialize

Minimality comes into play

What are good knowledge-base solutions?

First alternative: universal KB-solutions

But there exist some other KB-solutions desirable to materialize

Minimality comes into play

Given sets \mathcal{X} , \mathcal{Y} of instances:

▶ $X \equiv_{min} Y$ if X and Y coincide in the minimal instances under \subseteq

Definition

 (I_2, Γ_2) is a minimal KB-solution of (I_1, Γ_1) under \mathcal{M} if:

 $Mod(I_2, \Gamma_2) \equiv_{min} Sol_{\mathcal{M}}(Mod(I_1, \Gamma_1))$

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Given (I_1, Γ_1) and \mathcal{M} , when constructing a minimal KB-solution (I_2, Γ_2) we would like:

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1. Γ_2 to only depend on Γ_1 and \mathcal{M} :

 Γ_2 is safe for Γ_1 and $\mathcal M$

Given (I_1, Γ_1) and \mathcal{M} , when constructing a minimal KB-solution (I_2, Γ_2) we would like:

1. Γ_2 to only depend on Γ_1 and \mathcal{M} :

 Γ_2 is safe for Γ_1 and $\mathcal M$

Definition

 Γ_2 is safe for Γ_1 and \mathcal{M} , if for every I_1 there exists I_2 :

 (I_2, Γ_2) is a minimal KB-solution of (I_1, Γ_1) under \mathcal{M}

2. Γ_2 to be as informative as possible (thus minimizing the size of I_2):

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Γ₂ to be as informative as possible (thus minimizing the size of *l*₂):

Definition

 Γ_2 is *optimal-safe* if for every other safe set Γ' :

 $\Gamma_2 \models \Gamma'$

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To obtain algorithms for computing minimal KB-solutions, we need to specify the language used in knowledge bases.

Full st-tgd:

 $\forall \bar{x} \forall \bar{y} \left(\varphi(\bar{x}, \bar{y}) \to \psi(\bar{x}) \right)$

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► Full st-tgd:

 $\forall \bar{x} \forall \bar{y} \left(\varphi(\bar{x}, \bar{y}) \to \psi(\bar{x}) \right)$

Theorem (APR11)

There exists a polynomial-time algorithm that, given $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$, where Σ is a set of full st-tgds, and given a set Γ_1 of full tgds over \mathbf{S} , computes a set Γ_2 of second-order logic sentences over \mathbf{T} that is optimal-safe for Γ_1 and \mathcal{M} .

Unfortunately, first-order logic is no expressive enough.

Theorem (APR11)

There exist $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$, where Σ is a set of full st-tgds, and a set Γ_1 of full tgds over **S** such that:

no FO-sentence is optimal-safe for Γ_1 and \mathcal{M} .

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How can we deal with these problems in practice?

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How can we deal with these problems in practice?

 We need to restrict the language used to specify knowledge bases: Description logics [ABC11]

- Formalism for exchanging representations systems
- Applications to incomplete instances
- Applications to knowledge bases
- Concluding remarks

We can exchange more than complete data

We propose a general formalism to exchange *representation systems*

- Applications to incomplete instances
- Applications to knowledge bases

Next step: Apply our general setting to the Semantic Web

- Semantic Web data has nulls (blank nodes)
- Semantic Web specifications have rules (RDFS, OWL)

Lots of interesting problems to solve if knowledge bases are specified by means of description logics.

Better results can be obtained

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Thank you!

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Bibliography

- [ABC11] M. Arenas, E. Botoeva, D. Calvanese. Knowledge Base Exchange. DL 2011.
- [APR11] M. Arenas, J. Pérez, J. Reutter. Data Exchange beyond Complete Data. PODS 2011.
- [B03] P. A. Bernstein. Applying Model Management to Classical Meta Data Problems. CIDR 2003.
- [FKMP03] R. Fagin, P. G. Kolaitis, R. J. Miller, L. Popa. Data Exchange: Semantics and Query Answering. ICDT 2003.

Decision problem: CHECK-KB-SOL

Input: $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$, where Σ is a set of st-tgds (I_1, Γ_1) KB over \mathbf{S} with Γ_1 a set of tgds (I_2, Γ_2) KB over \mathbf{T} with Γ_2 a set of tgds

Output: Is (I_2, Γ_2) a KB-solution of (I_1, Γ_1) under \mathcal{M} ?

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Output: Is (I_2, Γ_2) a KB-solution of (I_1, Γ_1) under \mathcal{M} ?

Theorem (APR11)

CHECK-KB-SOL is undecidable (even for a fixed \mathcal{M}).

Undecidability is a consequence of using \exists in knowledge bases.

We need to restrict the input

$\operatorname{CHECK-FULL-KB-SOL:}$ $\Gamma_1,$ Γ_2 are assumed to be sets of full tgds

Theorem (APR11)

CHECK-FULL-KB-SOL *is EXPTIME-complete*.

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Theorem (APR11)

If $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma)$ is fixed:

CHECK-FULL-KB-SOL is $\Delta_2^P[O(\log n)]$ -complete.

 $\Delta_2^P[O(\log n)]$: P^{NP} with a logarithmic number of calls to the NP oracle.