

# Querying in the Age of Graph Databases and Knowledge Graphs

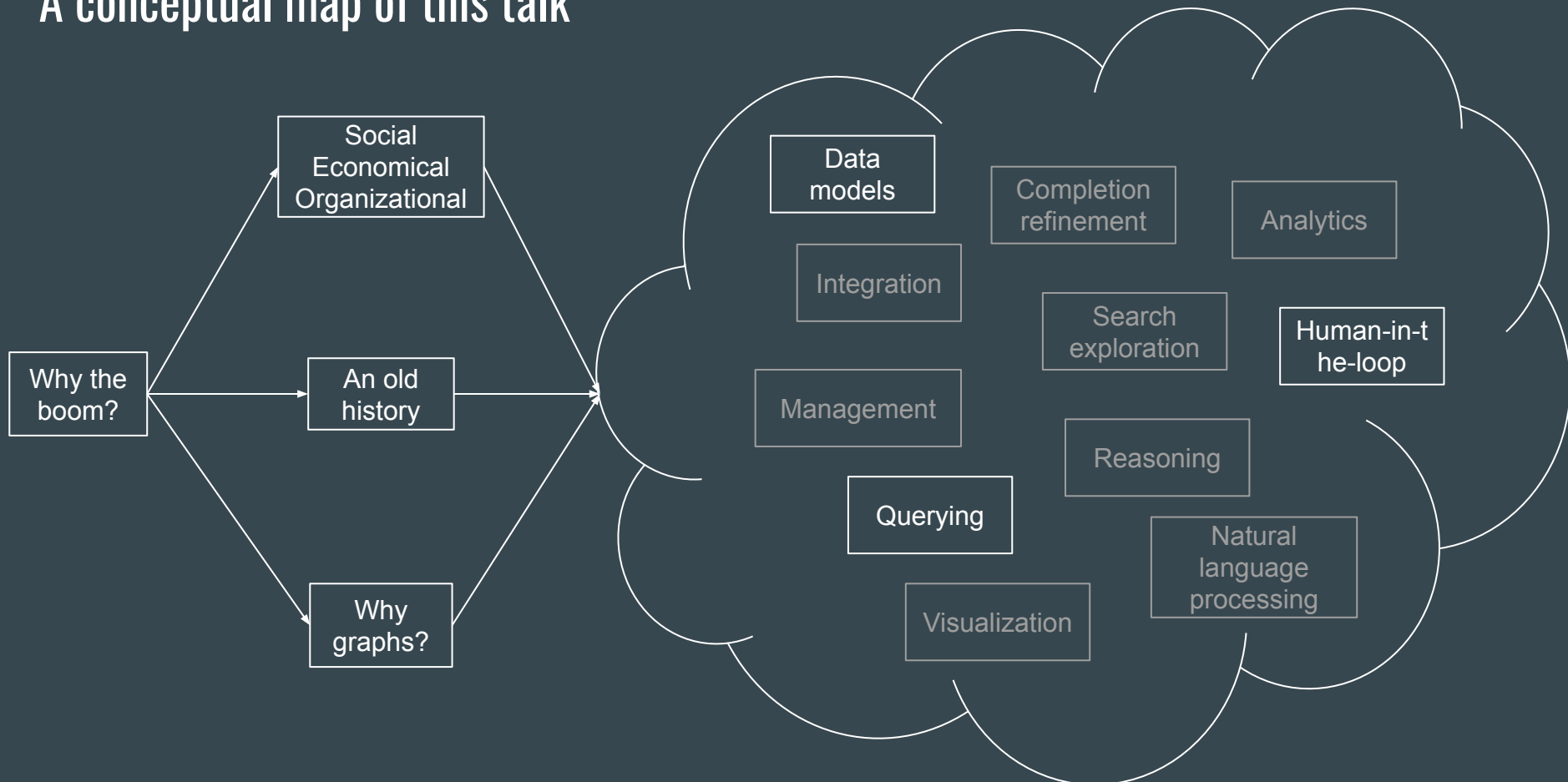


Marcelo Arenas, Claudio Gutierrez and Juan Sequeda

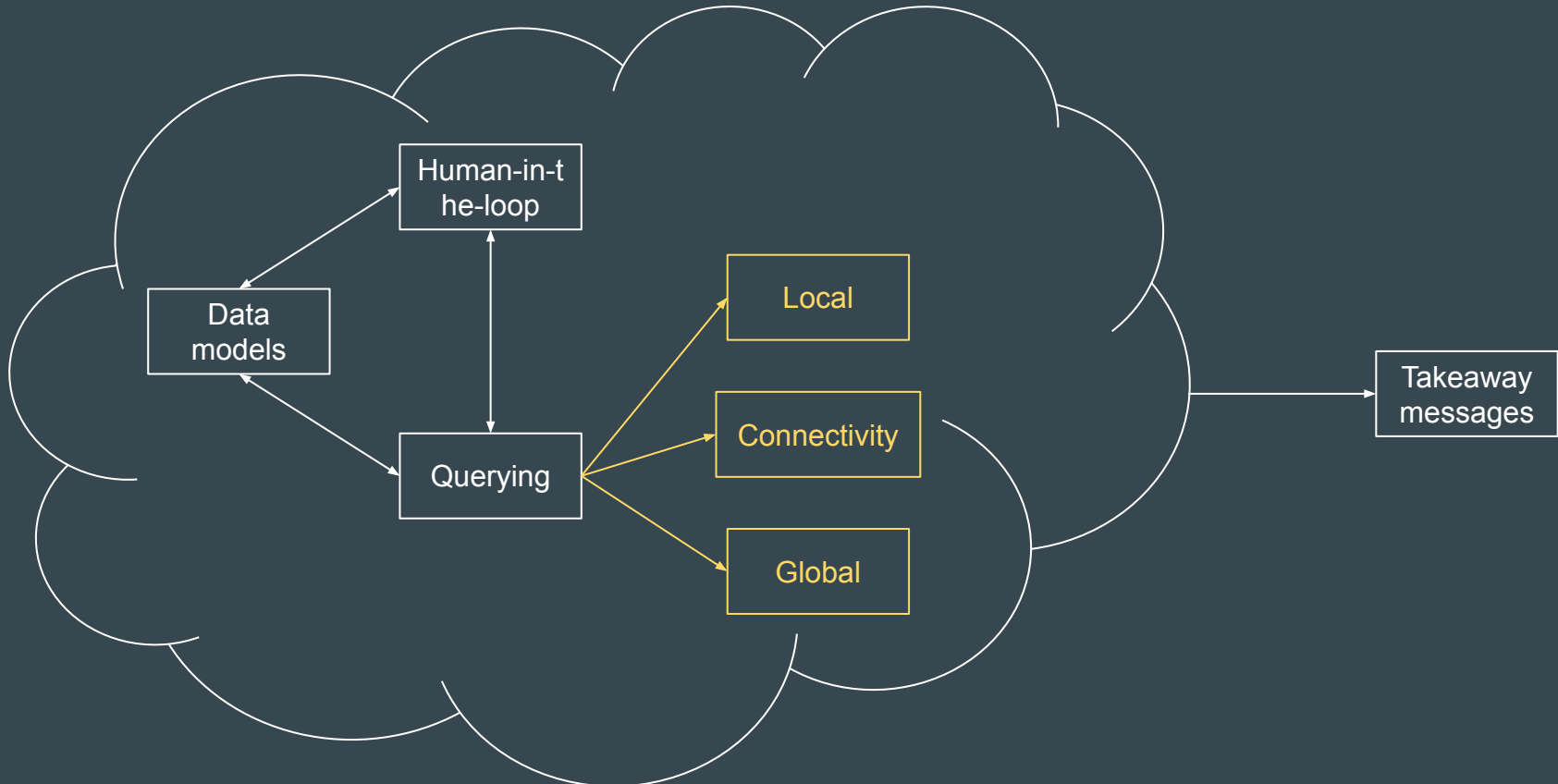
# A conceptual map of this talk



# A conceptual map of this talk



# A conceptual map of this talk



**A necessary digression:  
Why are we here?  
Why graphs everywhere?**

...

# Real World: Big Tech Giants

SEARCH

## Introducing the Knowledge Graph: things, not strings

Amit Singhal  
SVP, Engineering

Published May 16, 2012

Search is a lot about discovery—the basic human need to learn and broaden your horizons. But searching still requires a lot of hard work by you, the user. So today I'm really excited to launch the Knowledge Graph, which will help you discover new information quickly and easily.

## Apple is shoring up Siri for its next generation of intelligent devices

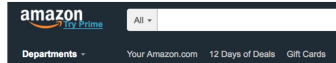
John Mannes @johnmannes / 3:43 pm CDT • May 16, 2017

Comment



## Product Graph

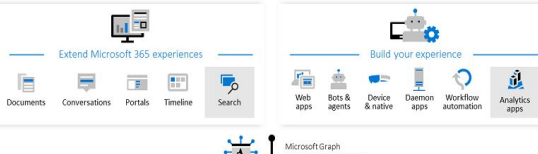
**Mission:** To answer any question about products and related knowledge in the world



Customers who bought this item also bought



## Microsoft 365 Platform



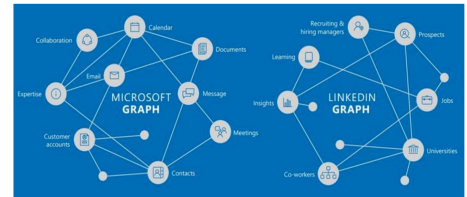
AI platform

	Data model	Size of the graph
Microsoft	The types of entities, relations, and attributes in the graph are defined in an ontology.	~2 billion primary entities, ~55 billion facts
Google	Strongly typed entities, relations with domain and range inference	1 billion entities, 70 billion assertions
Facebook	All of the attributes and relations are structured and strongly typed, and optionally indexed to enable efficient retrieval, search, and traversal.	~50 million primary entities, ~500 million assertions
eBay	Entities and relation, well-structured and strongly typed	Expect around 100 million products, >1 billion triples
IBM	Entities and relations with evidence information associated with them.	Various sizes. Proven on scales documents >100 million, relationships >5 billion, entities >100 million

## Building The LinkedIn Knowledge Graph

Qi He October 6, 2016

Share Tweet f Share

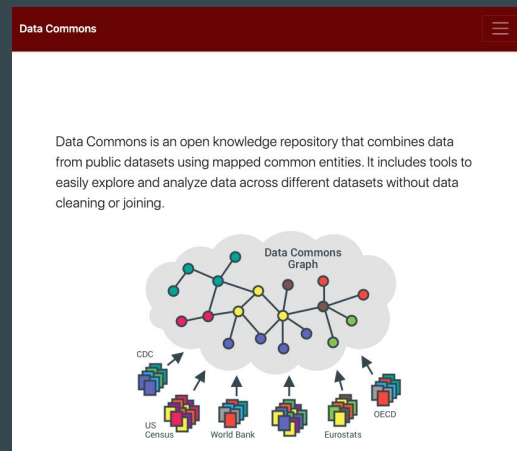


Authors: Qi He, Bee-Chung Chen, Deepak Agarwal

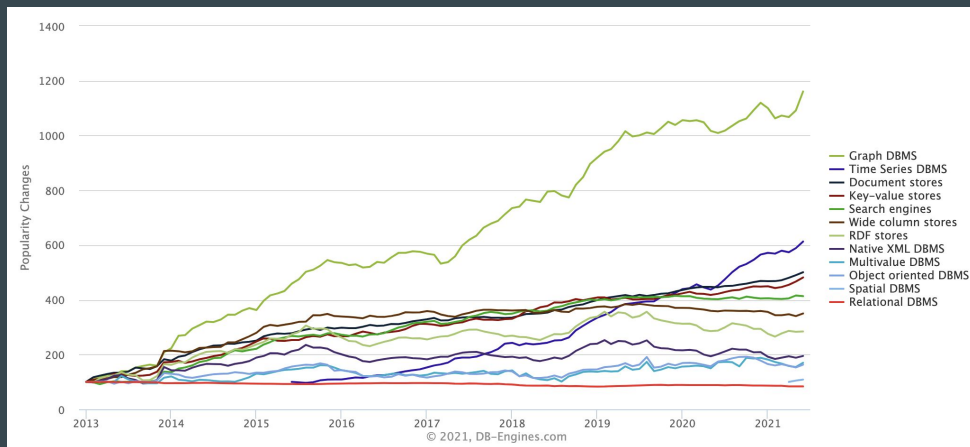
# Real World: Large KG



NSF's  
Open Knowledge  
Network



# Real World: Market Growth



[https://db-engines.com/en/ranking\\_categories](https://db-engines.com/en/ranking_categories)

## Trend No. 8: Graph relates everything

Graph forms the foundation of modern data and analytics with capabilities to enhance and improve user collaboration, machine learning models and explainable AI. Although graph technologies are not new to data and analytics, there has been a shift in the thinking around them as organizations identify an increasing number of use cases. In fact, as many as 50% of Gartner client inquiries around the topic of AI involve a discussion around the use of graph technology.

## Market Guide for Graph Database Management Solutions

Published 24 May 2021

By 2025, graph technologies will be used in 80% of data and analytics innovations, up from 10% in 2021, facilitating rapid decision making across the enterprise.

<https://www.gartner.com/doc/4001808>

## Gartner Top 10 Data and Analytics Trends for 2021

<https://www.gartner.com/smarterwithgartner/gartner-top-10-data-and-analytics-trends-for-2021/>



# Real World: Not just the Big Tech Giants



Most content management done with aid of knowledge graph.  
Coordinates journalist's work. Powers article recommendations



“Intelligent Content Ecosystem” (videos, games, articles, ...)  
Meaningful product and article recommendations, age ratings across multiple jurisdictions and languages, along with justifications

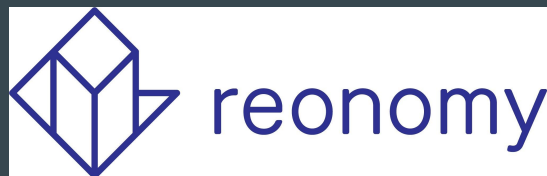


Member profiles from single system, near real-time, including contact timeline and care-path recommendations.  
Claimed \$150 million per year savings

# Real World: Data Product Companies too



Supports \$2bn marketing agency for all customer insights  
Integration of 100s of millions of datapoints from 1000s of sources  
Development efficiency: “do in 12 hours what we couldn’t in 6 months”



“Unprecedented Products”: ownership portfolio of commercial real-estate  
Development efficiency: new dataset live in 5 days with junior dev

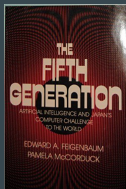
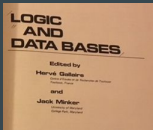
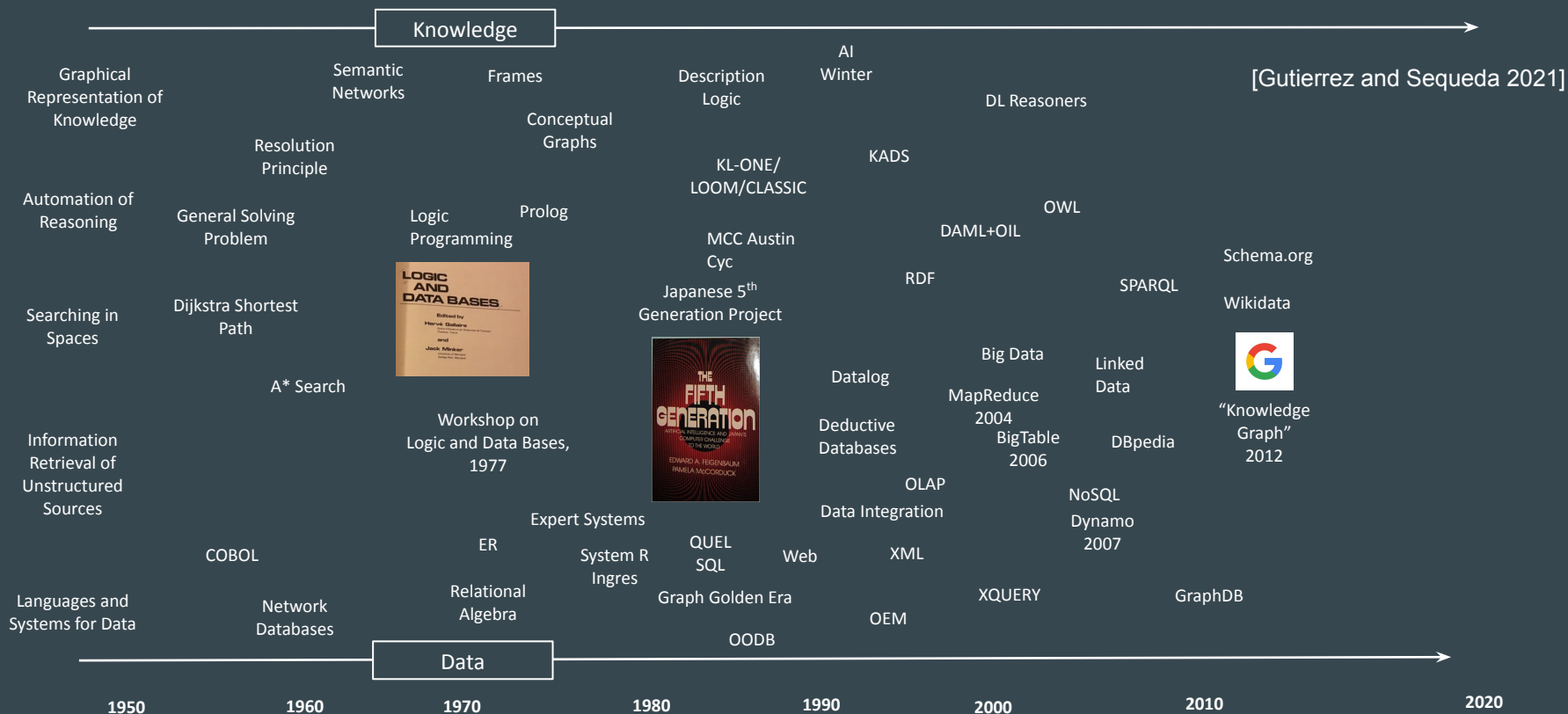


Multiple data products based on unstructured web-base data: news, organizations, people

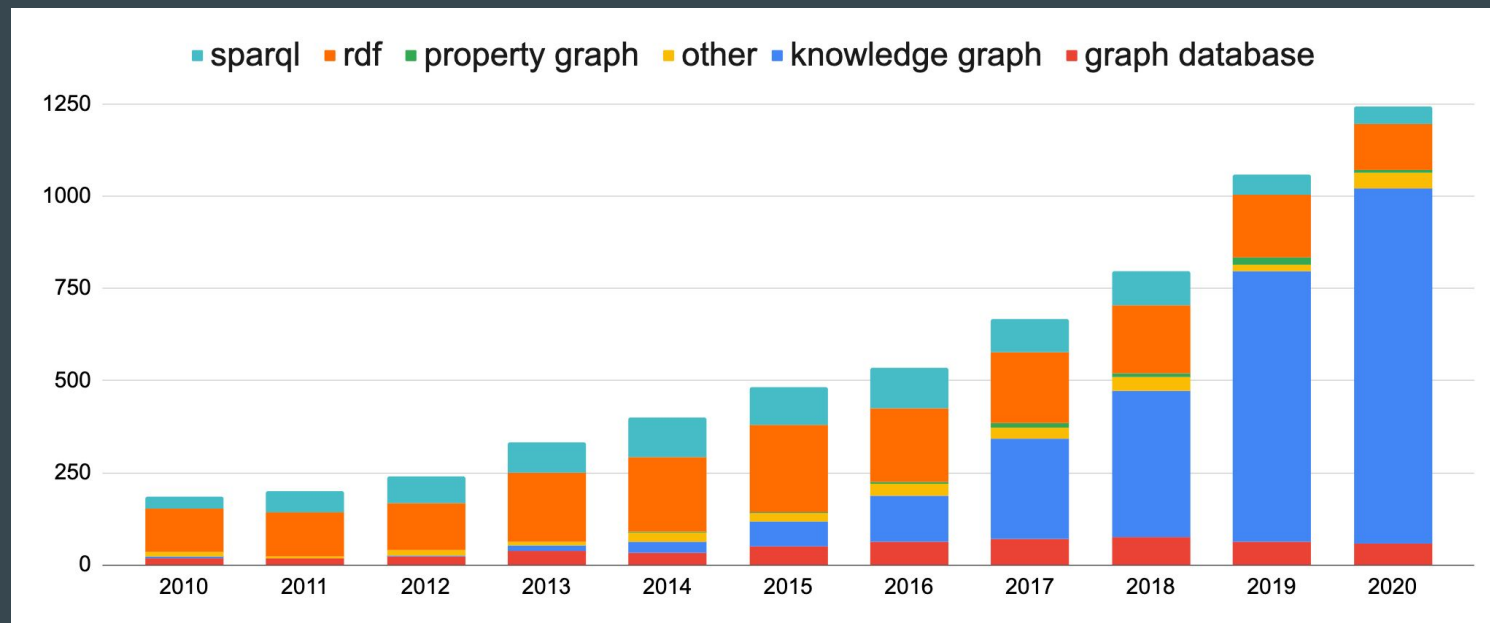


Gathers data from many sources to create a private Small & Medium Business data product

# A bit of history about knowledge and data

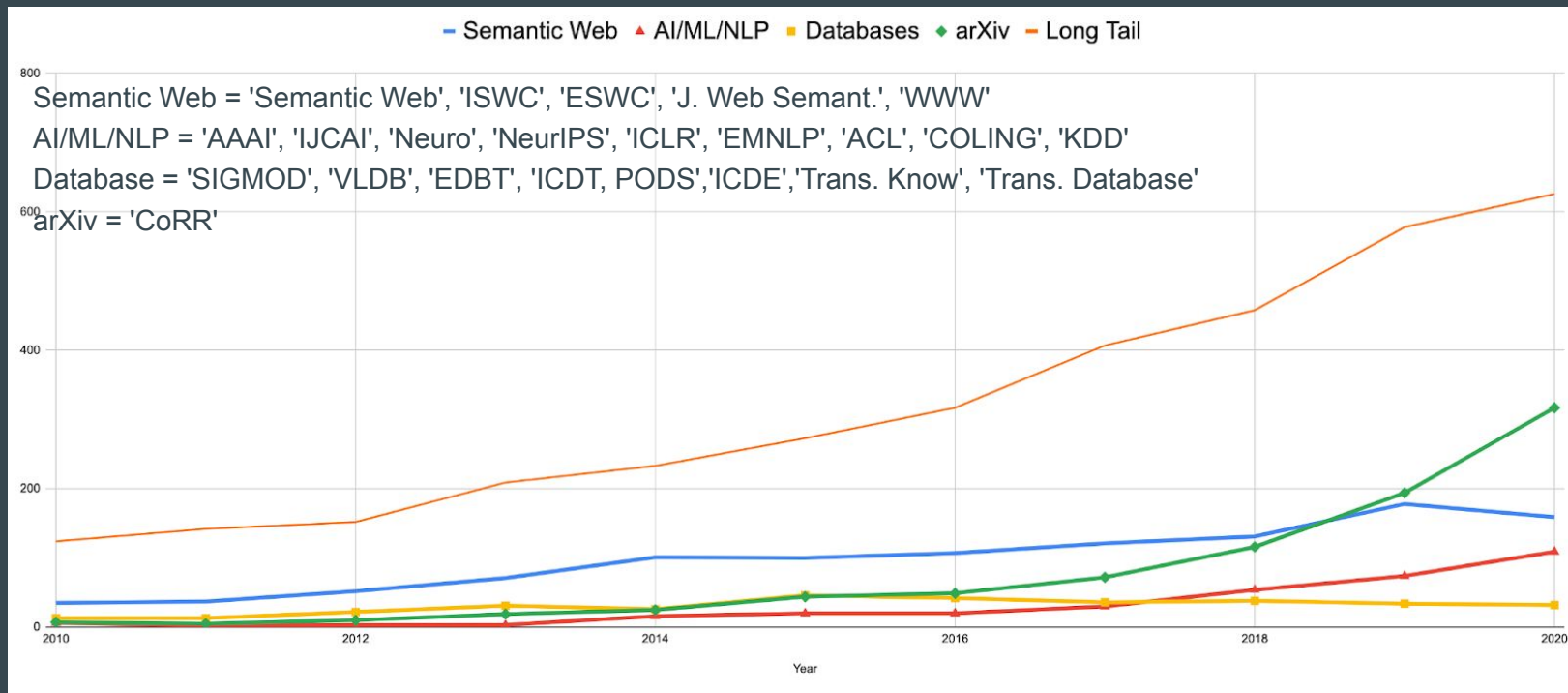


# KG types of papers (per DBLP)



Number of papers where sparql/rdf/knowledge graph/graph database/property graph appears in the title

# Where are KG papers being published (per DBLP)



# Summary of graph data today, past and future

- Real World
  - Knowledge graphs are not just for the Tech Giants
  - KG and Graph Databases are already in many places and it will keep growing
- Rich History
  - This isn't new, it's been boiling up for a while
- Academic Interest
  - Steady academic interest

**Why did graphs become so relevant for data  
and knowledge?**

...

# What is new today?

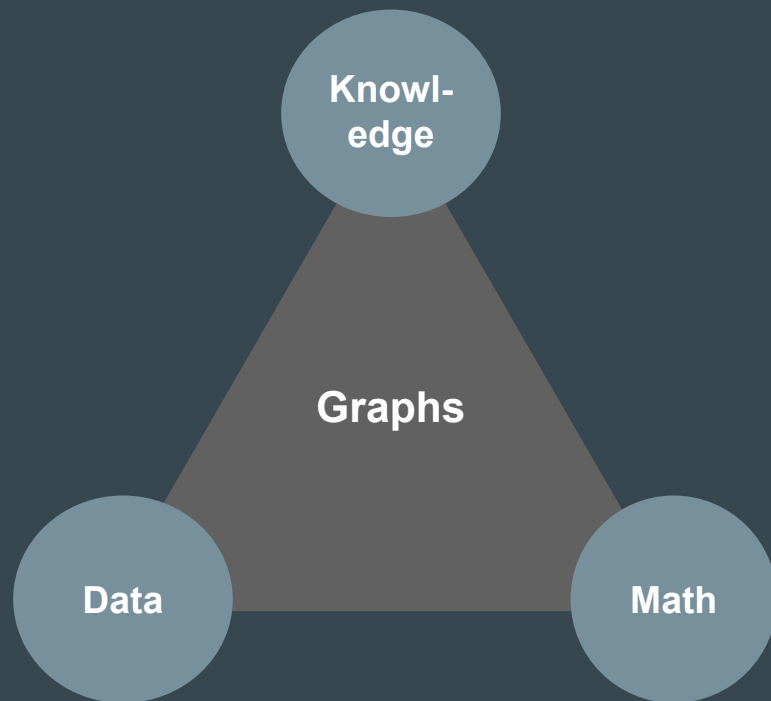
1. Graphs were long ago recognized as prime representation media for **knowledge**
2. The network-like intrinsic characteristic of **data** was also well known
3. Graphs are well known and studied mathematical objects

**The novelty today is the integration of these three previously disjoint trends**



# An outline of this part

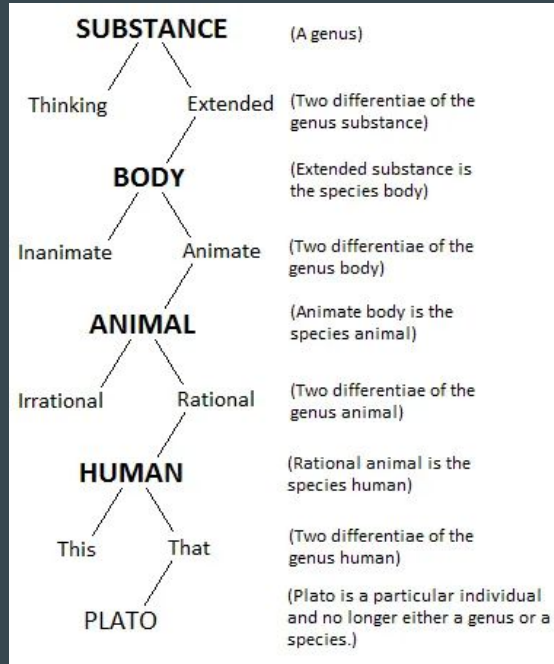
- Graphs and knowledge
- Graphs and data
- Graphs as mathematical structures



# Knowledge and graphs: an old history

- Aristotle and categories
- Lull and tree of knowledge
- Routes in maps
- Chemical graphs
- Semantic Networks
- ...
- Graph databases
- Knowledge graphs

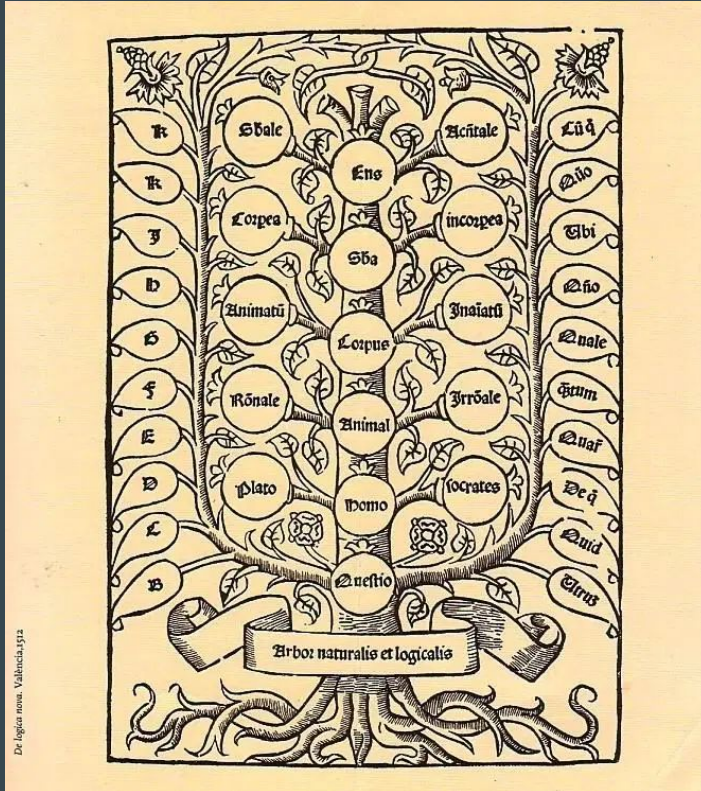
# Tree-shaped visualization of Aristotle categories



Porphyrian Tree (left, 4th century) and its “deletion” on the left (16th century).  
(This and following illustrations taken from Scott B. Weingart:  
<https://scottbot.net/knowledge/>)

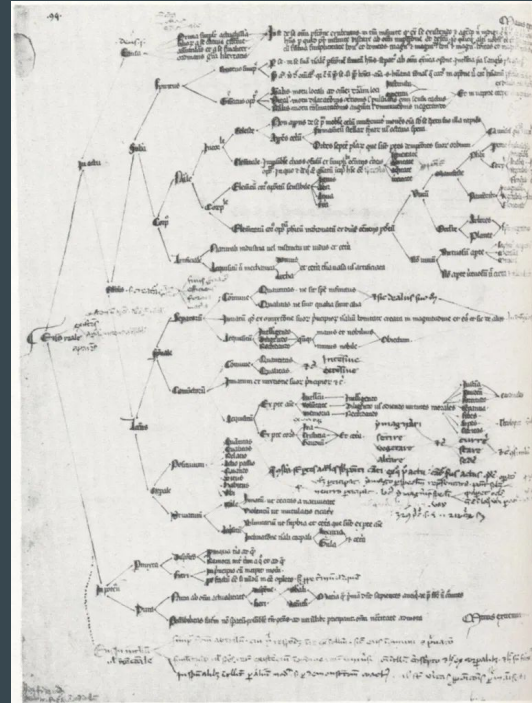
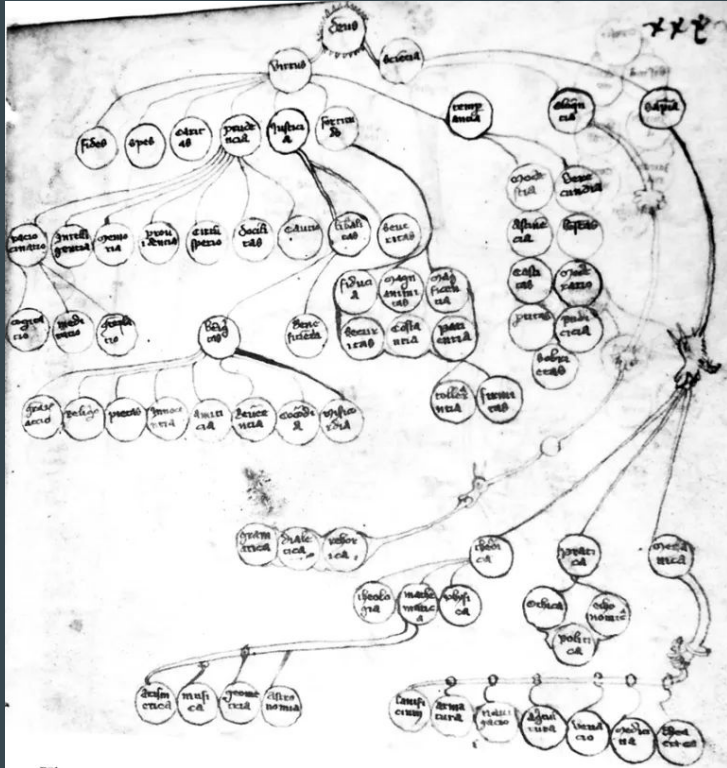


# An ordered tree



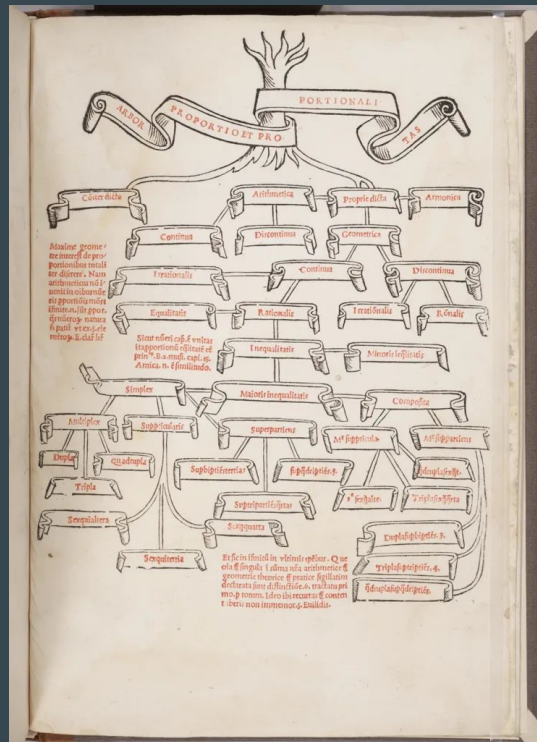
Tree of Knowledge (Ramon Llull)

# Problems with the material form of the representation

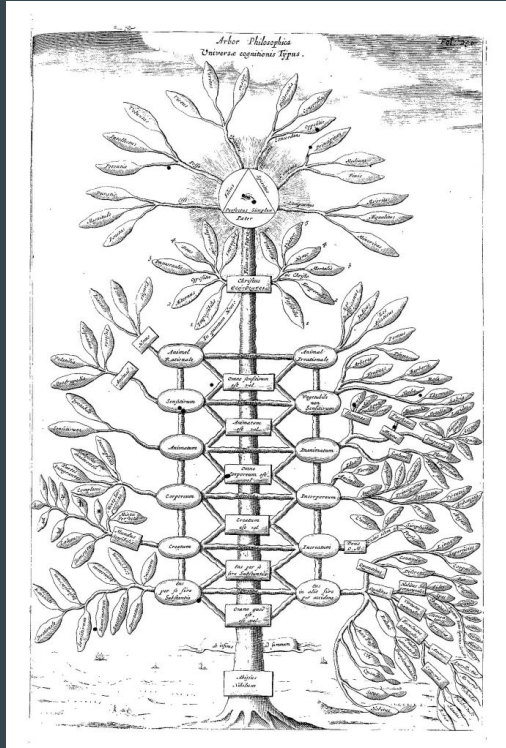


14th century diagrams

# Non-digital XML: Italy and the Andes (circa 15th century)



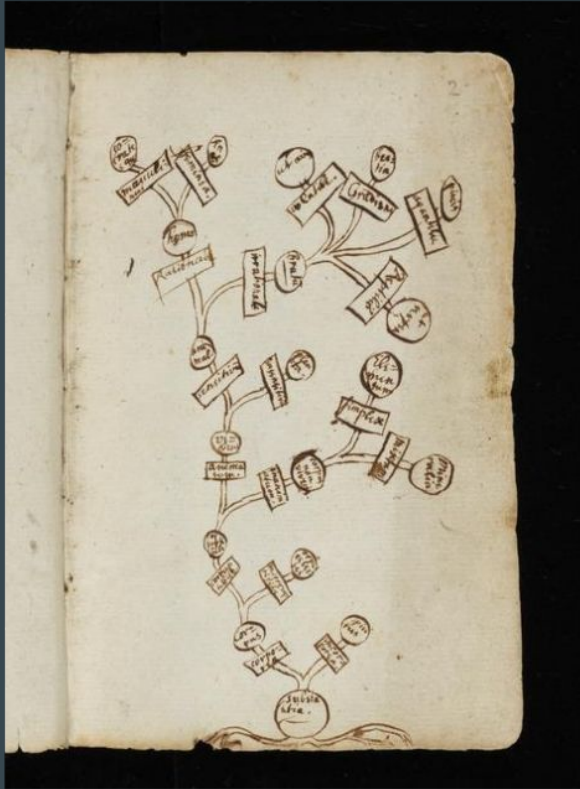
# Representation of different types of nodes, edges and complex graph structure



Athanasius Kircher's Philosophical tree representing all branches of knowledge (1669)



# Diagrams in Newton's notebook

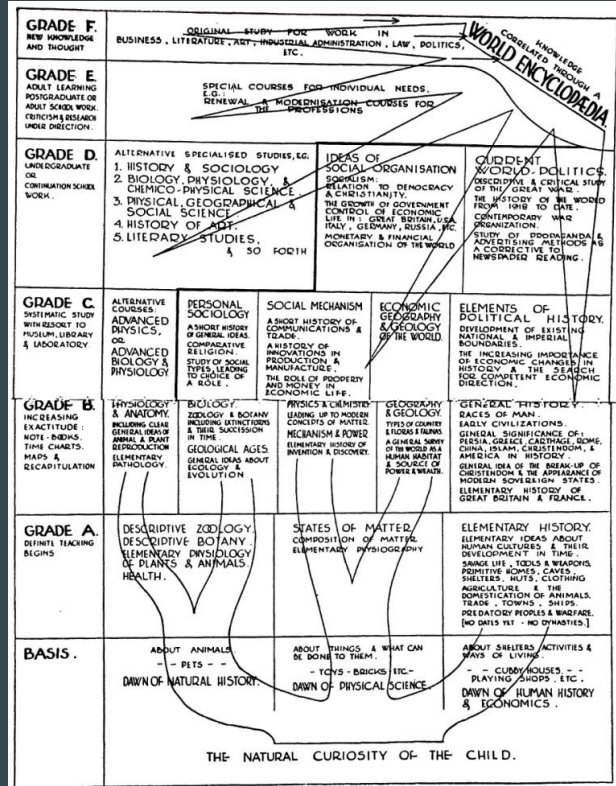


Newton's 'Trinity College Notebook' (MS Add. 3996)

It was used by him as an undergraduate, from about 1661 to 1665.

<http://cudl.lib.cam.ac.uk/view/MS-ADD-03996/5>

# 1938's conceptual graph



H.G. Wells describing how students ought to learn in 1938.

# Tree-like polymer topologies

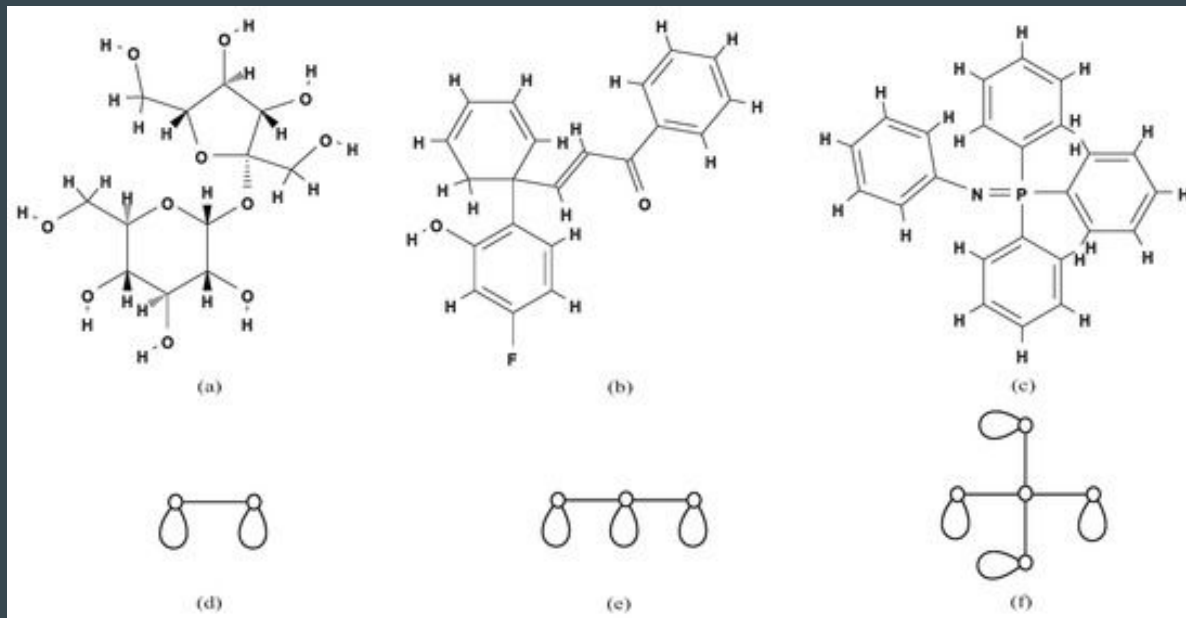
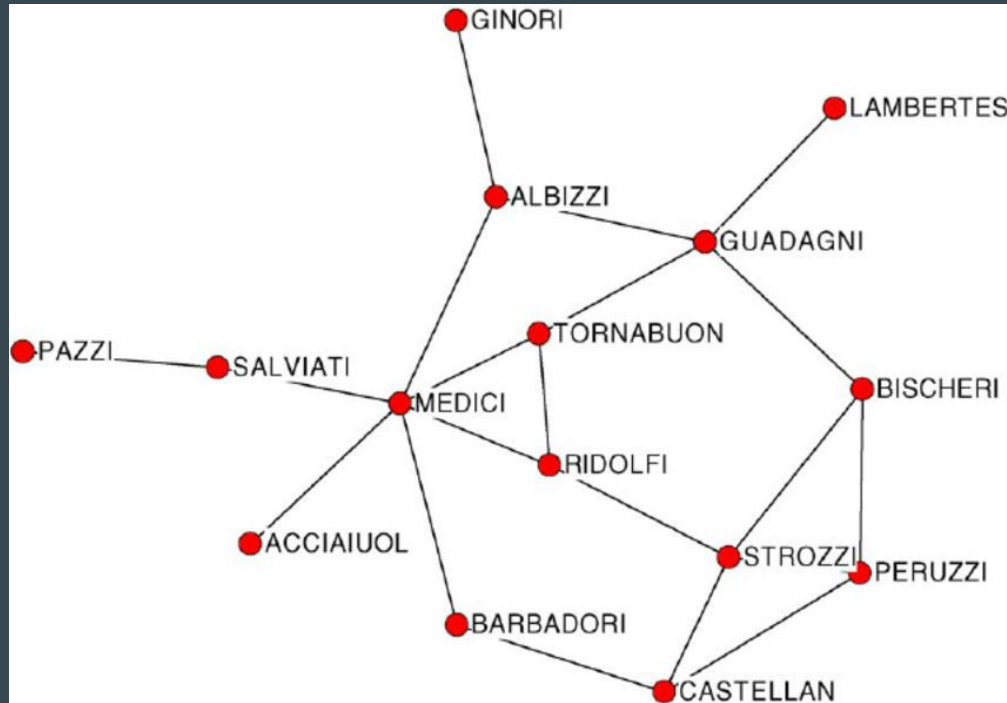


Image in: Azam, N.A.; Shurbevski, A.; Nagamochi, H. Enumerating Tree-Like Graphs and Polymer Topologies with a Given Cycle Rank. *Entropy* **2020**

# Social / semantic / linguistic networks



Florentine families' network

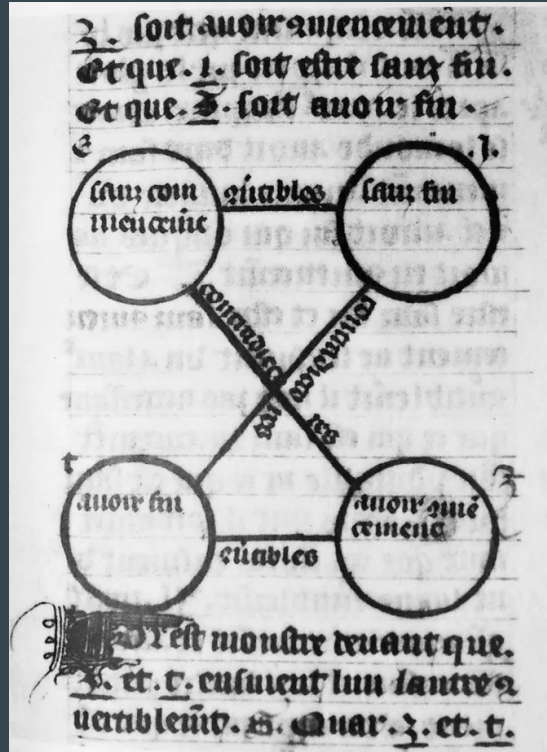
Image taken from: Borgatti, Stephen. (2005). Centrality and Network Flow. *Social Networks*. 27. 55-71.

# Graphs and logic

“...all deductive reasoning, even simple syllogism, involves an element of observation; namely, deduction consists in constructing an icon or diagram the relations of whose parts shall present a complete analogy with those of the parts of the object of reasoning, of experimenting upon this image in the imagination, and of observing the result so as to **discover unnoticed and hidden relations** among the parts”

Ch. S. Peirce. *The Algebra of Logic*, 1885

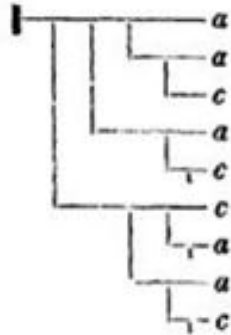
# Early connection of graphs and Logic



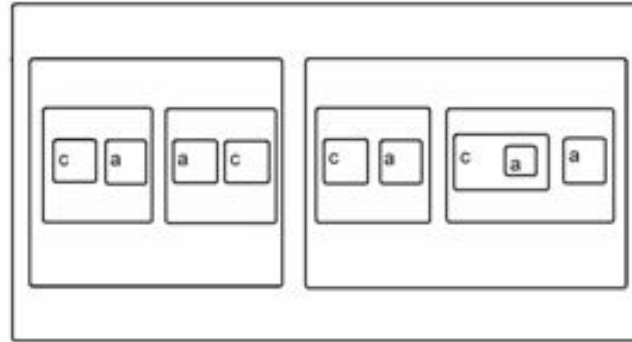
Oresme's 14th century square of opposition.

# Diagrammatic logic representations

Frege :



Peirce :



Russell (et Whitehead) :

$\sim c \supset a . \supset . \sim a \supset c : \supset . \sim c \supset a . \supset : c \supset a . \supset a$

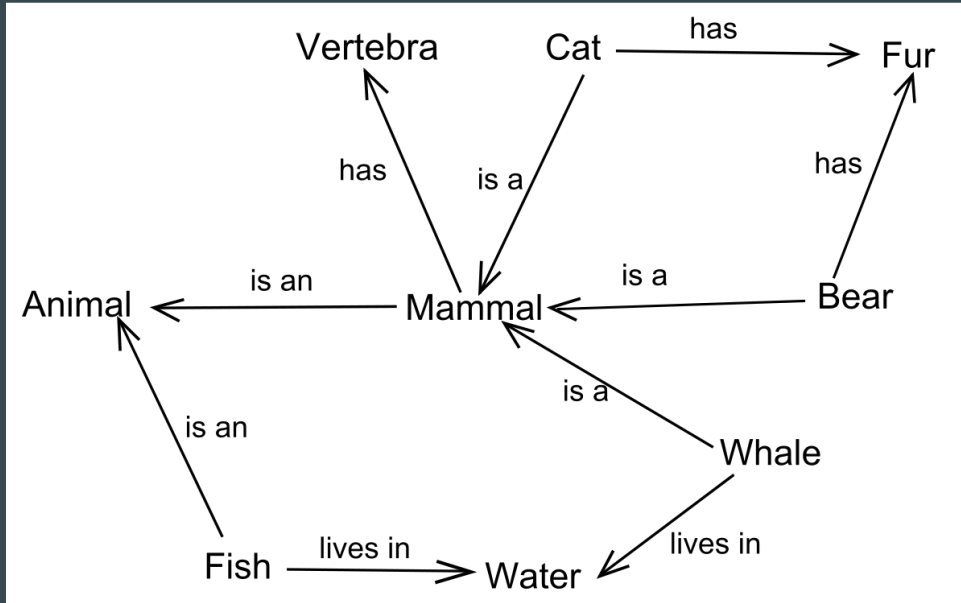
Lukasiewicz :

CCCNcaCNacCCNcaCCcaa

Irving H. Anellis

<https://ininet.org/how-peircean-was-the-fregean-revolution-in-logic-1.html?page=7>

# Semantic networks: logic specifications in a diagrammatic form



has(Mammal, Vertebra)

is\_a(Cat, Mammal)

$\forall x \forall y \forall z \text{ is\_a}(x,y) \wedge \text{has}(y,z) \Rightarrow \text{has}(x,z)$



# The unusual effectiveness of diagrams to represent knowledge

Fundamental ideas behind this linkage between graphs and knowledge:

- Simple way of abstracting facets of real life and processes
- Easy visualization for humans
- Simple to operationalize and communicate
- Open the possibility to find new relations that were not explicitly present in the original model or its parts

# Graphs as a simple formal model for diagrams

Graphs represent a very simple and widespread conceptual model:

- ***Entities*** (represented as nodes)
- ***Relationships*** (represented as edges)

# Graphs as a simple formal model for diagrams

- The model can be easily formalized in mathematical terms
- The human perception may be possible to automatize to a great extent
- It is a good idea to scale this model of reasoning beyond human capabilities

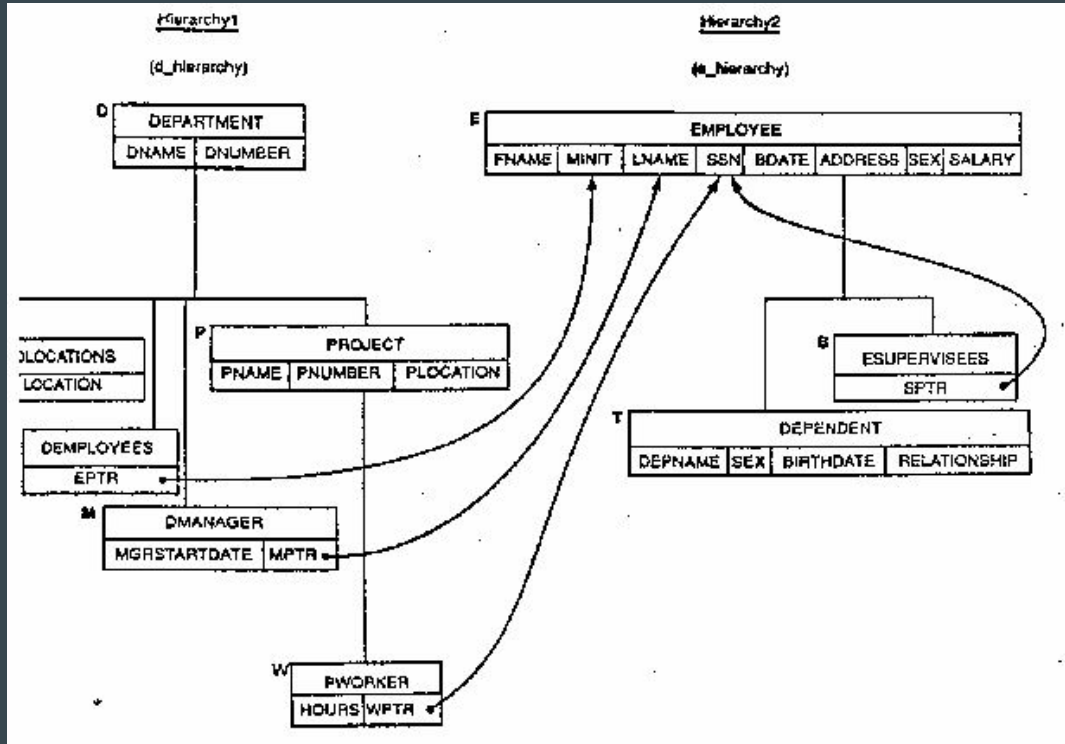
# Data and graphs

Problems already discussed:

- Complex diagrams are difficult to handle in physical terms
- Many particular metadata (thus difficult to interoperate, integrate or extend)
- Paper make them static (as images)

Idea with the advent of the digital: **give flexibility to the physical representation**

# A digital/data representation for graphs



“Primitive” versions:

- discrete
- formal

This led to:

- clearly defined data types
- nodes as records
- relations as pointers among registers

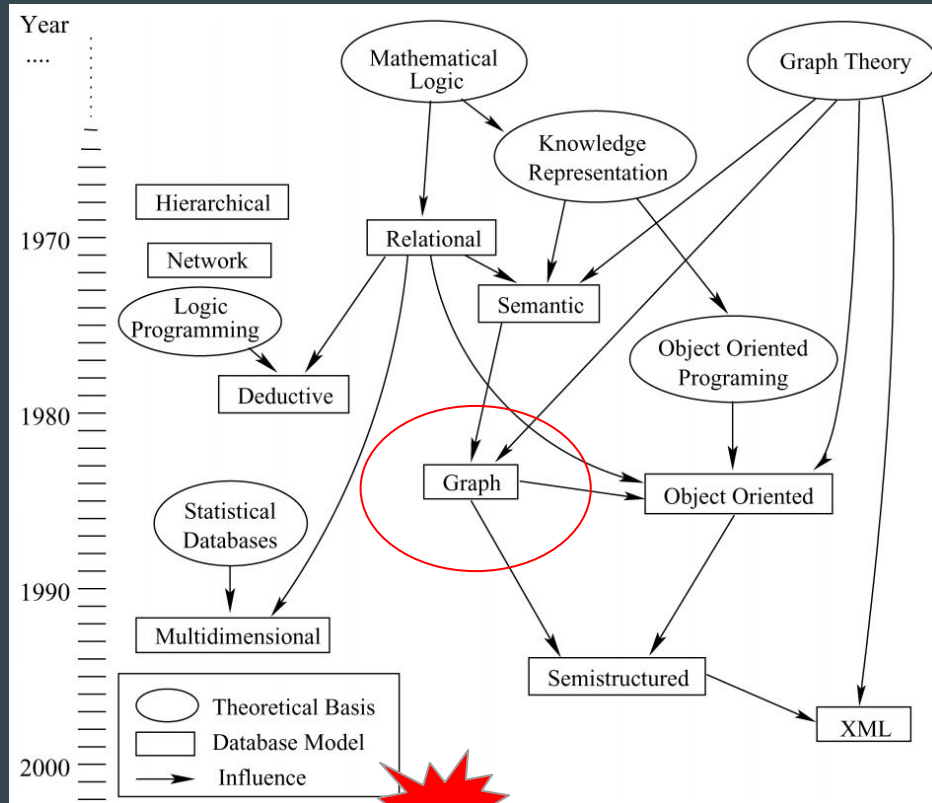
# The advent of graph data models

Second wave: attempt to implement the idea of **separation of concerns**

- user view graphs
- implementation

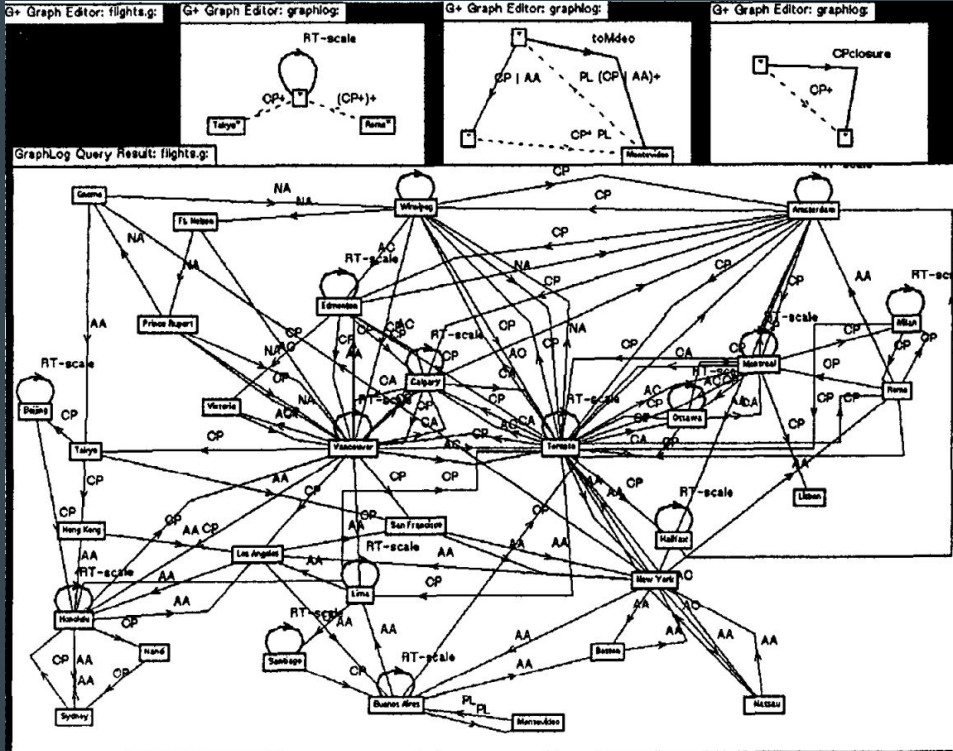
Almost succeeded in the 1980's: golden era of graph databases

# The advent of graph data models



[Diagram by A. Mendelzon  
In: Angles and Gutierrez 2008]

# The advent of graph data models: Problems: hardware, software, visualization



[Consens and Mendelzon 1990]



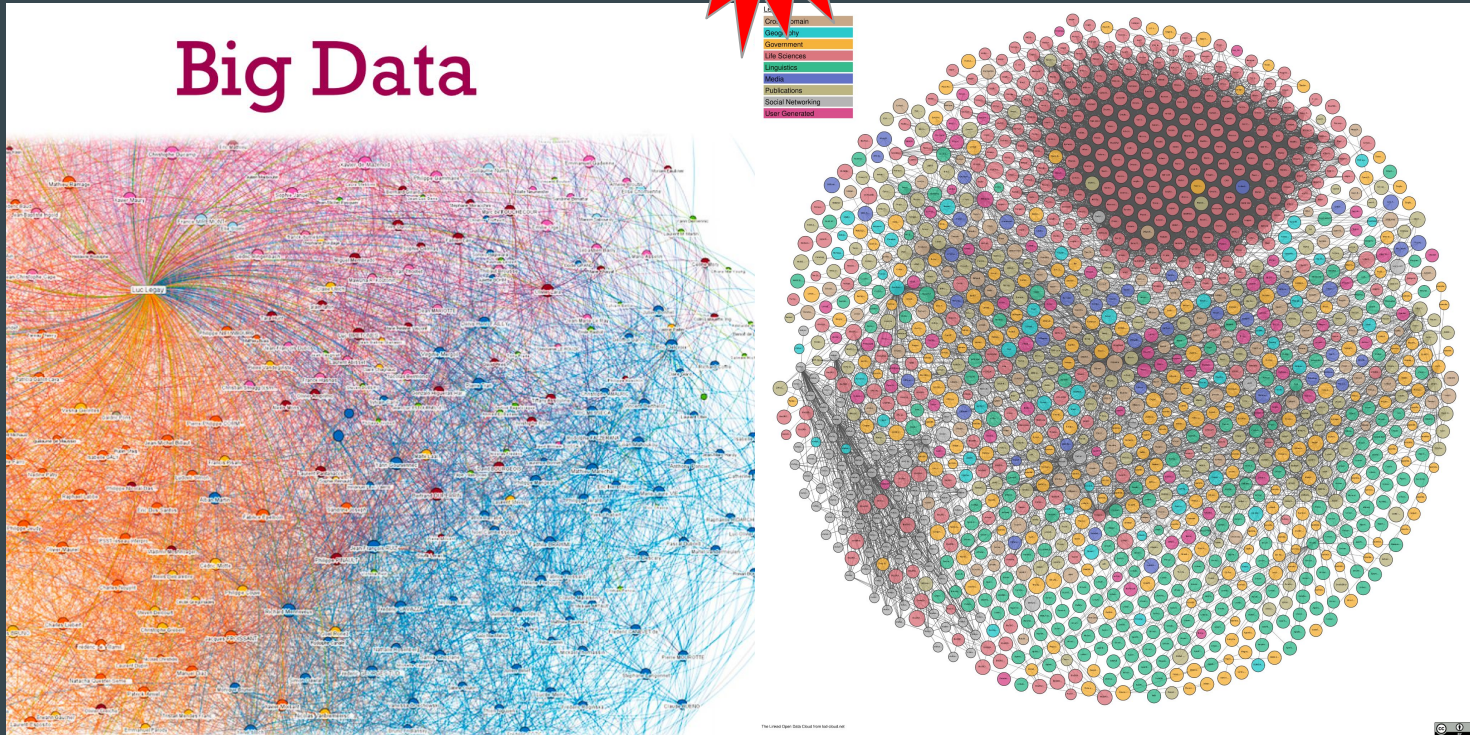
# Why did graph databases become necessary?

- Scale (millions of node and edges)
  - Thus, Peirce's insights not anymore true
- Versatile visualization software
  - Back some of Peirce's insights
- Incorporation of different types
  - Particularly multimedia: images, sound, video

## What is preserved?

- Simplicity of representation
- Simplicity of integration and extension

# An upheaval to graph databases



# Graphs as mathematical structures

Extraordinary simple building blocks, and richness of representation for the construction of complex structures.

To manage appropriately large graphs we need to understand [Chung 2010]:

- What are the basic structure of such large networks?
- How do they evolve?
- What are the underlying principles that dictate their behavior?
- How are subgraphs related to the large (and often incomplete) host graphs?
- What are the main graph invariants that capture the myriad of properties of large graphs?

# Some fundamental tools

The Toolbox includes [Chung 2010]:

- Combinatorial and probabilistic methods
- Spectral methods

And for non-symmetric structures:

- General random graph theory for any given degree distribution
- Percolation in general host graphs
- PageRank for representing quantitative correlations
- Game aspects

# The geometry of graphs

Three main types of properties can be distinguished in graphs:

- **Local properties:** nodes and neighborhoods
- **Connectivity properties:** paths and their regular and logical expressions
- **Global properties:** networks analysis, analytics in general

**Querying:**

**What are new challenges?**

**What are new techniques?**

...

# A conceptual view of querying graphs

- **Local properties**

Extracting nodes from a graph: first-order logic with bounded resources and graph neural networks

- **Connectivity properties**

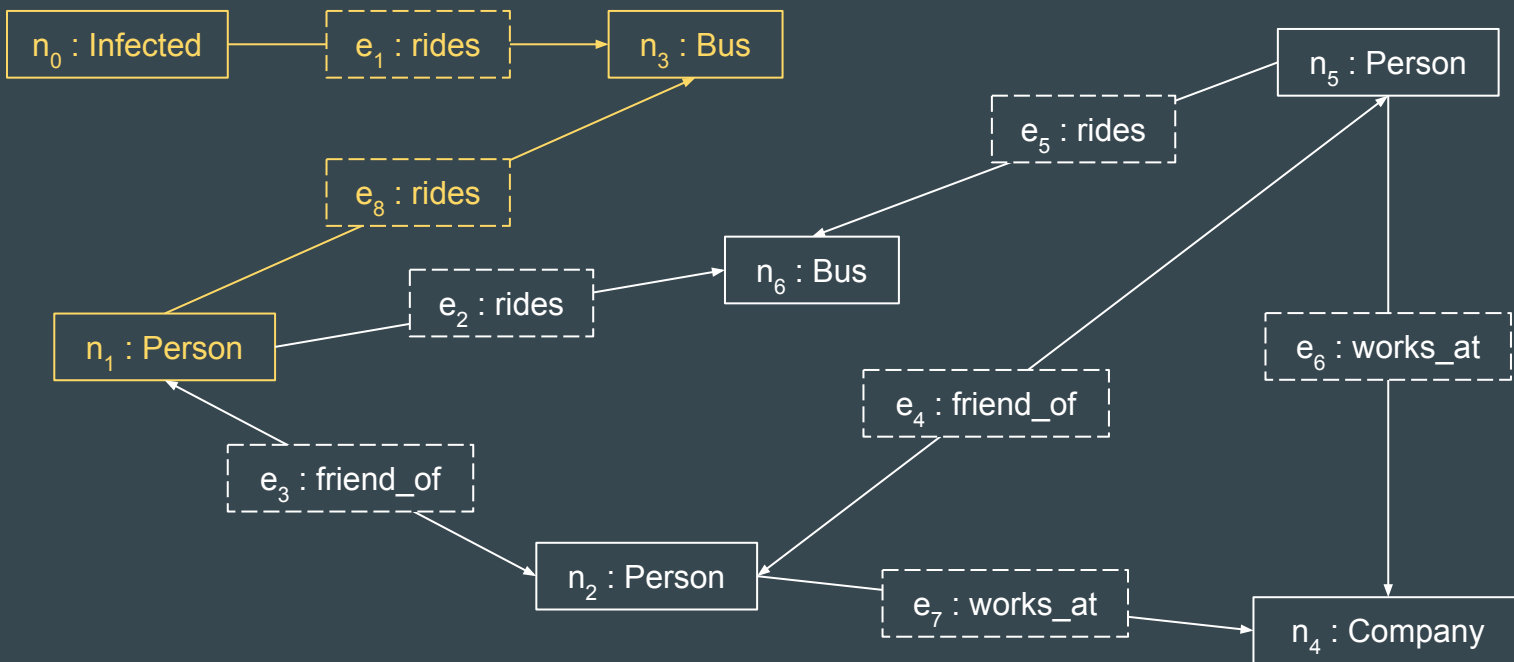
Extracting paths from a graph: approximation and uniform generation  
Paths as first-class citizens

- **Global properties**

Explainable AI and the search of a declarative language for interpretability

# Extracting nodes from a graph: an old problem

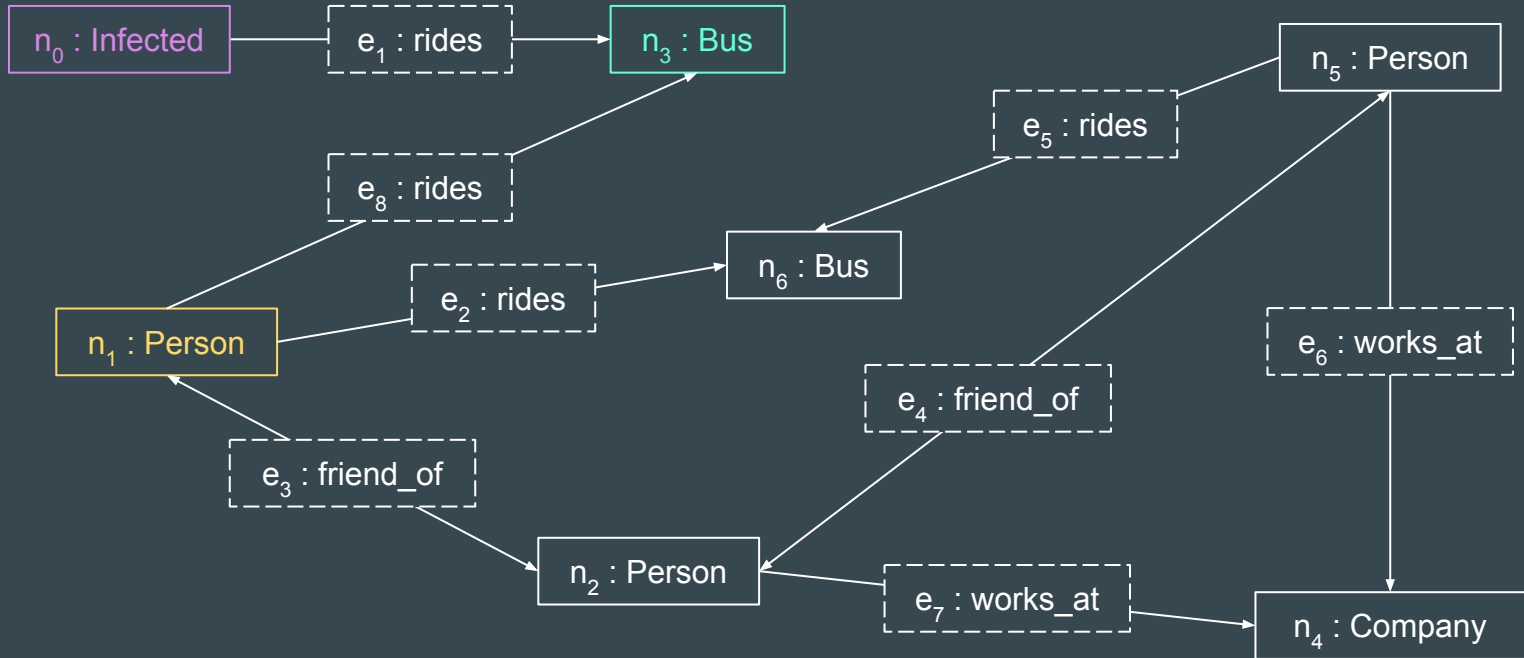
The notion of close contact: `?Person/rides/?Bus/rides-/?Infected`





# An old idea: use first order-logic (FO) as a query language

$\text{Person}(x) \wedge \exists y [\text{rides}(x,y) \wedge \text{Bus}(y) \wedge \exists z (\text{rides}(z,y) \wedge \text{Infected}(z))]$



## Also an old idea: use FO with bounded resources

$\text{Person}(x) \wedge \exists y [\text{rides}(x,y) \wedge \text{Bus}(y) \wedge \exists x (\text{rides}(x,y) \wedge \text{Infected}(x))]$

Only two variables are needed

- Only the values of these variables need to be stored
- No need to store partial results from joins of arbitrary size

# Evaluating FO with bounded resources

$\text{Person}(x) \wedge \exists y [\text{rides}(x,y) \wedge \text{Bus}(y) \wedge \exists x (\text{rides}(x,y) \wedge \text{Infected}(x))]$

Person
x
$n_1$
$n_2$
$n_6$

rides	
x	y
$n_0$	$n_3$
$n_1$	$n_3$
$n_1$	$n_6$
$n_5$	$n_6$

Bus
y
$n_3$
$n_6$

rides	
x	y
$n_0$	$n_3$
$n_1$	$n_3$
$n_1$	$n_6$
$n_5$	$n_6$

Infected
x
$n_0$

# Evaluating FO with bounded resources

$\text{Person}(x) \wedge \exists y [\text{rides}(x,y) \wedge \text{Bus}(y) \wedge \exists x (\text{rides}(x,y) \wedge \text{Infected}(x))]$

Person
x
$n_1$
$n_2$
$n_6$

rides	
x	y
$n_0$	$n_3$
$n_1$	$n_3$
$n_1$	$n_6$
$n_5$	$n_6$

Bus
y
$n_3$
$n_6$

x	y
$n_0$	$n_3$

# Evaluating FO with bounded resources

$\text{Person}(x) \wedge \exists y [\text{rides}(x,y) \wedge \text{Bus}(y) \wedge \exists x (\text{rides}(x,y) \wedge \text{Infected}(x))]$

Person
x
$n_1$
$n_2$
$n_6$

rides	
x	y
$n_0$	$n_3$
$n_1$	$n_3$
$n_1$	$n_6$
$n_5$	$n_6$

Bus
y
$n_3$
$n_6$

y
$n_3$

# Evaluating FO with bounded resources

$\text{Person}(x) \wedge \exists y [\text{rides}(x,y) \wedge \text{Bus}(y) \wedge \exists x (\text{rides}(x,y) \wedge \text{Infected}(x))]$

Person
x
$n_1$
$n_2$
$n_6$

rides	
x	y
$n_0$	$n_3$
$n_1$	$n_3$
$n_1$	$n_6$
$n_5$	$n_6$

y
$n_3$

# Evaluating FO with bounded resources

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Person
x
$n_1$
$n_2$
$n_6$

x	y
$n_0$	$n_3$
$n_1$	$n_3$

# Evaluating FO with bounded resources

$\text{Person}(x) \wedge \exists y [\text{rides}(x,y) \wedge \text{Bus}(y) \wedge \exists x (\text{rides}(x,y) \wedge \text{Infected}(x))]$

Person	x
x	n <sub>0</sub>
n <sub>1</sub>	n <sub>1</sub>
n <sub>2</sub>	
n <sub>6</sub>	

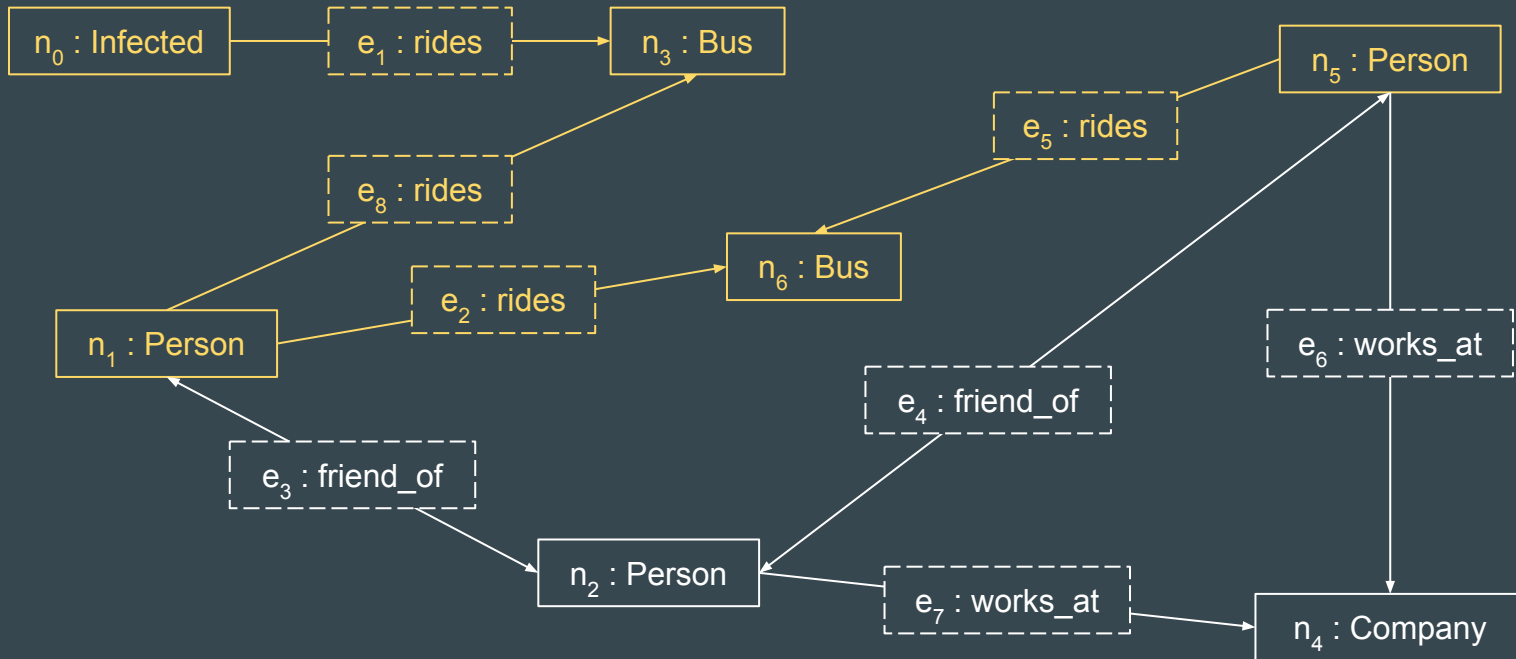


# Evaluating FO with bounded resources

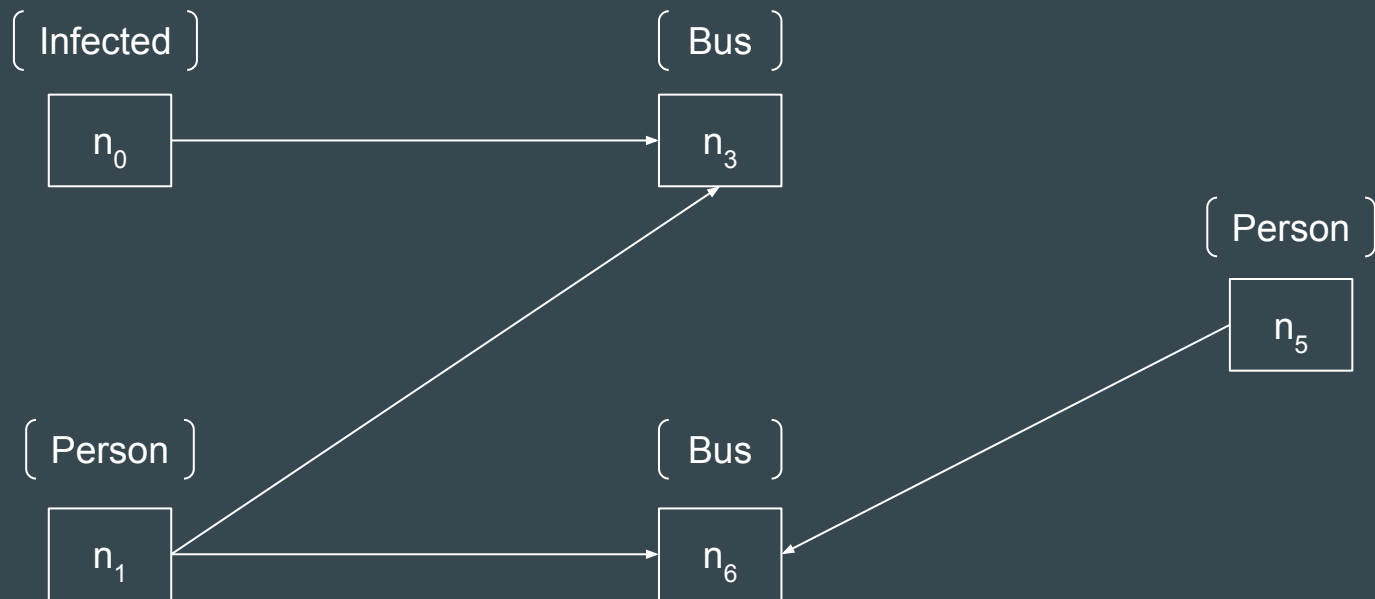
$\text{Person}(x) \wedge \exists y [\text{rides}(x,y) \wedge \text{Bus}(y) \wedge \exists x (\text{rides}(x,y) \wedge \text{Infected}(x))]$

$x$
$n_1$

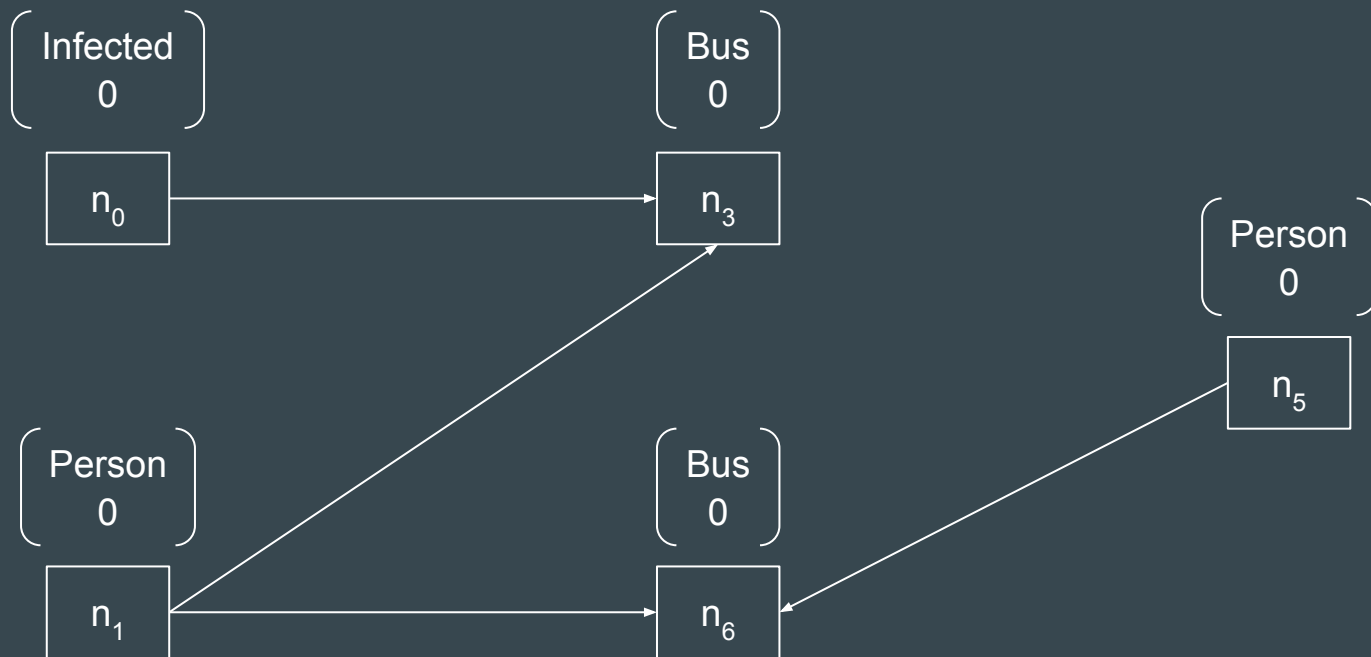
# On the other side: Graph neural networks (GNNs)



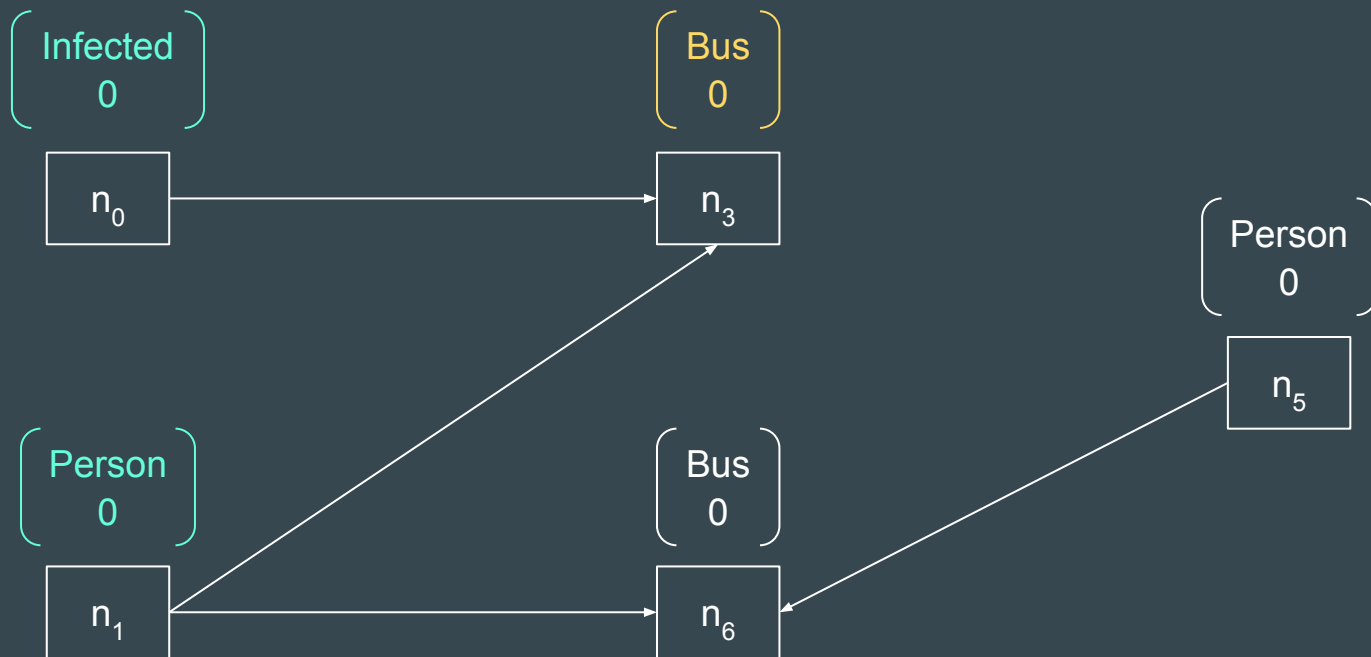
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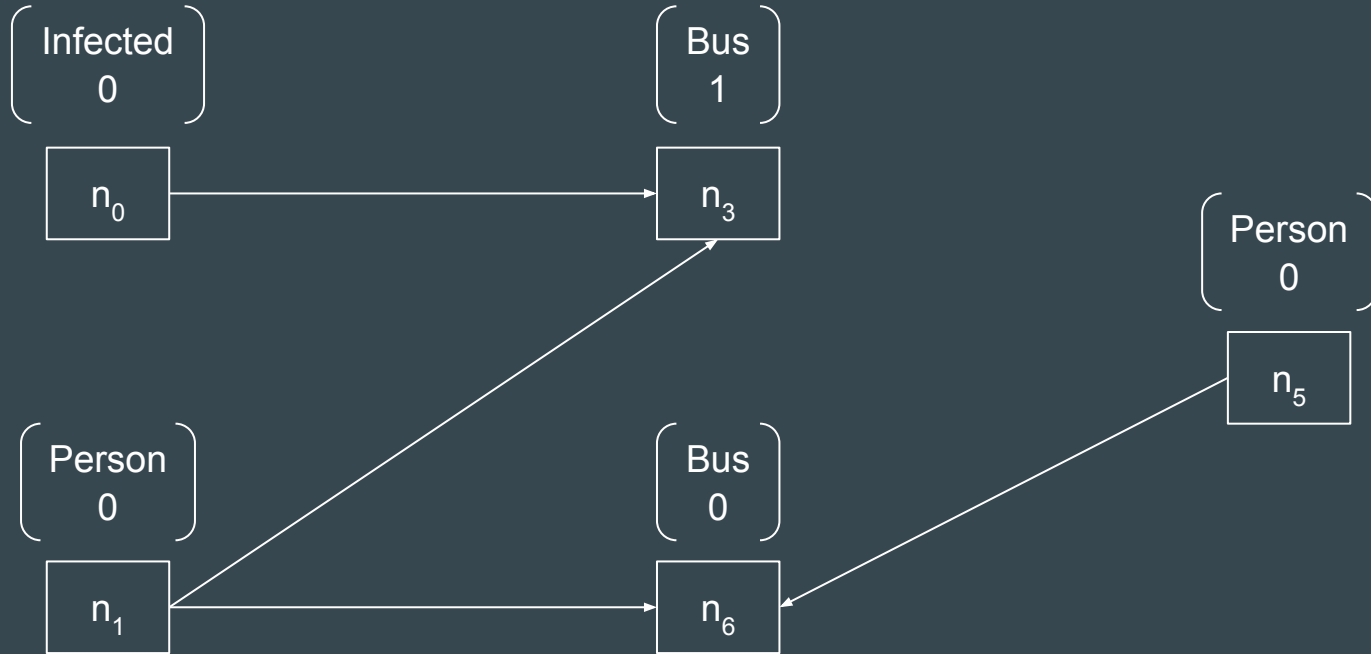
# Processing by layers in GNNs: the input



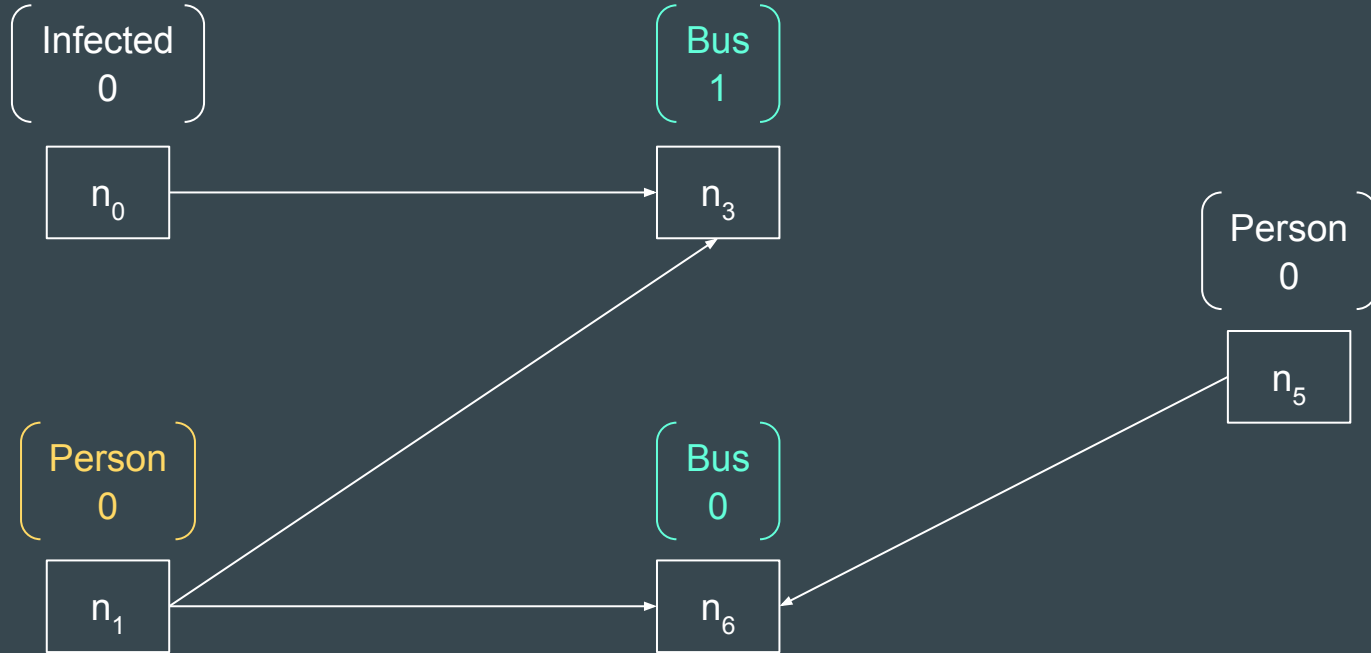
# Computing the first layer



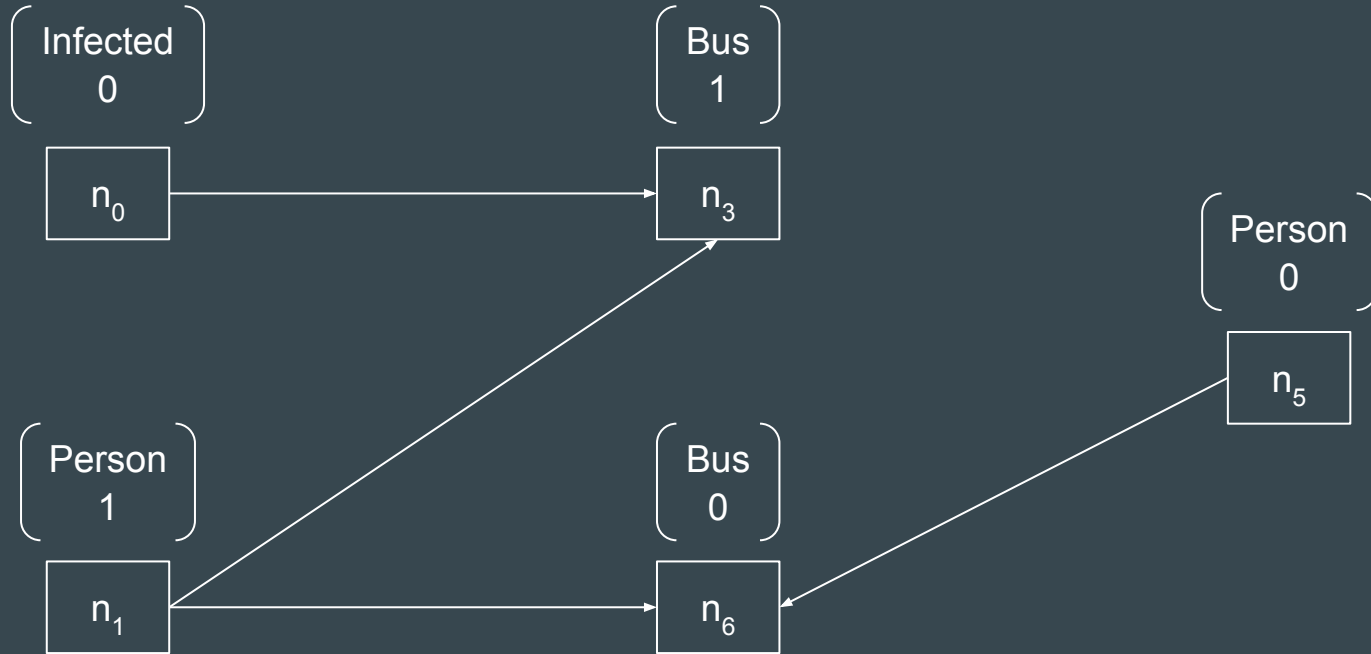
# The result of the first layer



# Computing the next layer



# The result of second layer





# The architecture of GNNs

$u^{(i)}$ : vector of features of node  $u$  at layer  $i$

- $u^{(0)}$  is the vector of features from the input graph

$$u^{(i+1)} = \text{COMB}( u^{(i)}, \text{AGG}(\{ \{ v^{(i)} \mid u \text{ and } v \text{ are neighbors in } G \} \} ) )$$

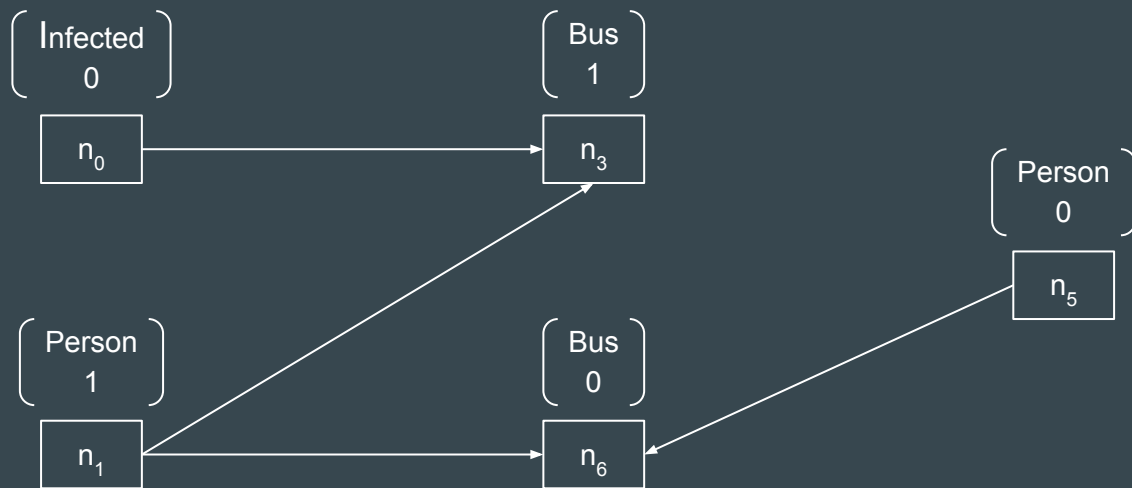
If  $k$  is the last layer:  $\text{CSL}(u^{(k)})$  is the result for node  $u$

# The architecture of GNNs

?Person/rides/?Bus/rides-/?Infected

$$\text{CSL} \left( \begin{array}{c} \text{Person} \\ 1 \end{array} \right) = 1$$

$$\text{CSL} \left( \begin{array}{c} \text{Person} \\ 0 \end{array} \right) = 0$$



# How are the previous paradigms related?

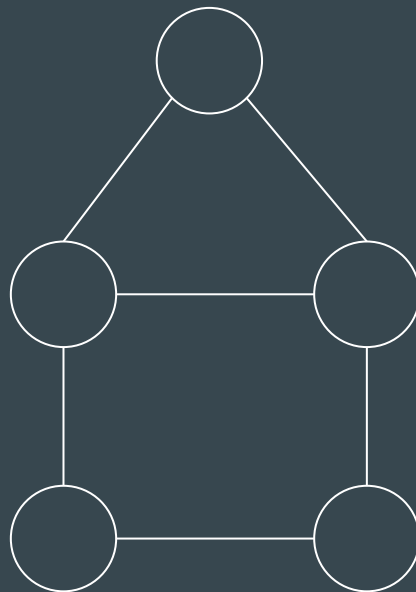
A new idea: the Weisfeiler-Lehman (WL) graph isomorphism test makes the connection

Two alternative points of view:

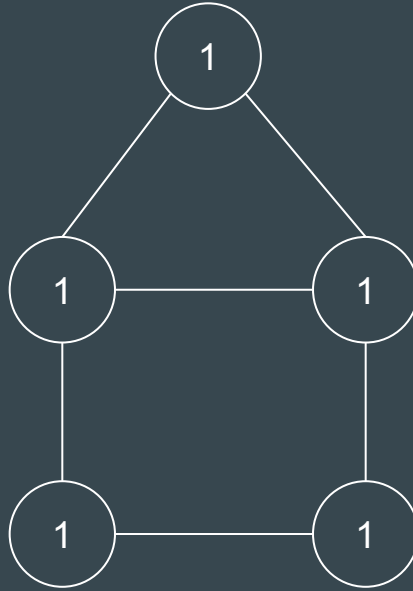
- First-order logic is a declarative query language, with a well-known and studied inference mechanism
- GNNs are a popular classification paradigm, with a growing number of algorithms and techniques to *learn* and implement them

# The bridge: WL test for graph isomorphism

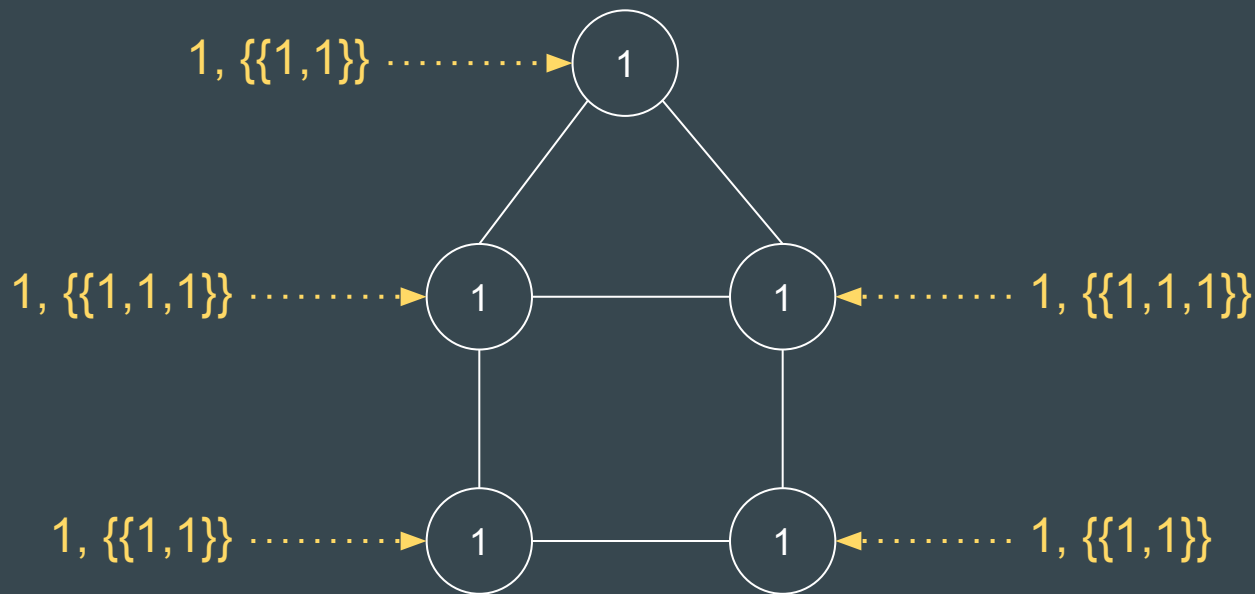
We will construct a canonical  
representation  
(1-dimensional test)



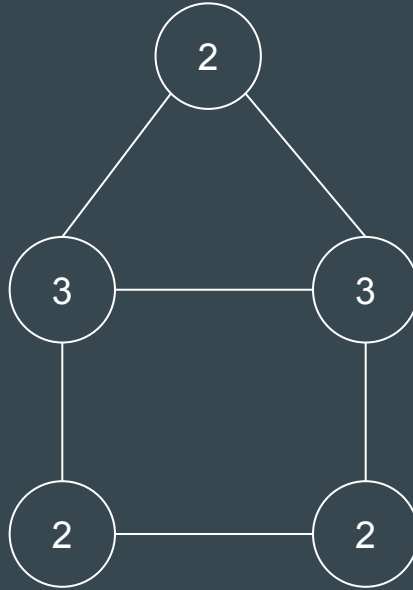
# The WL test for graph isomorphism



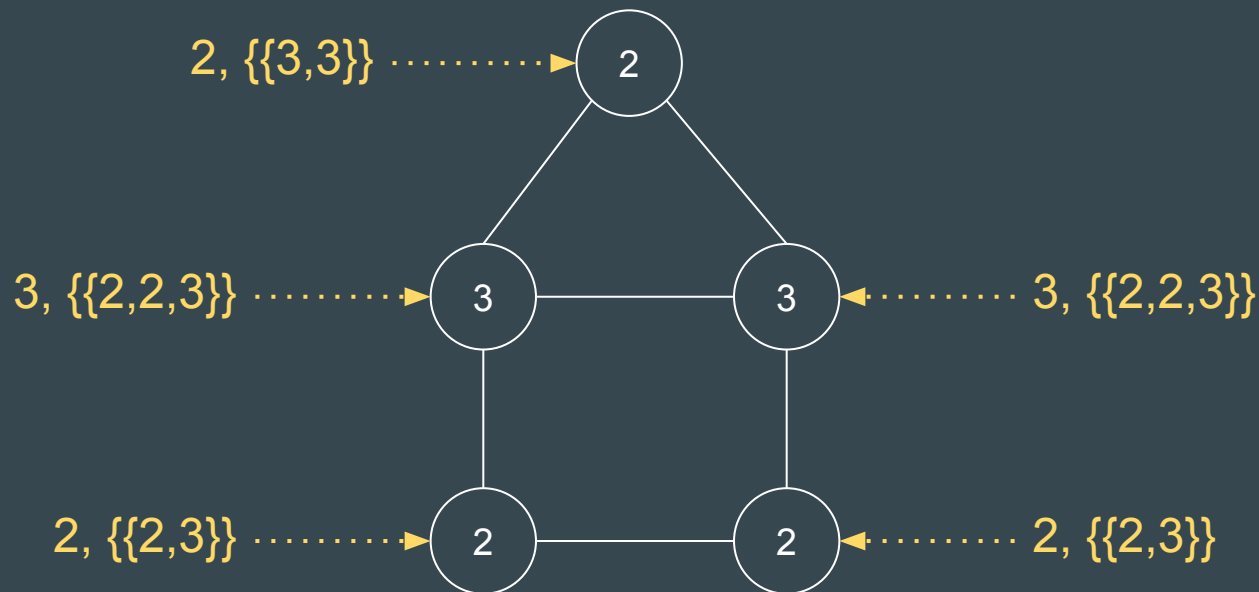
# The WL test for graph isomorphism



# The WL test for graph isomorphism

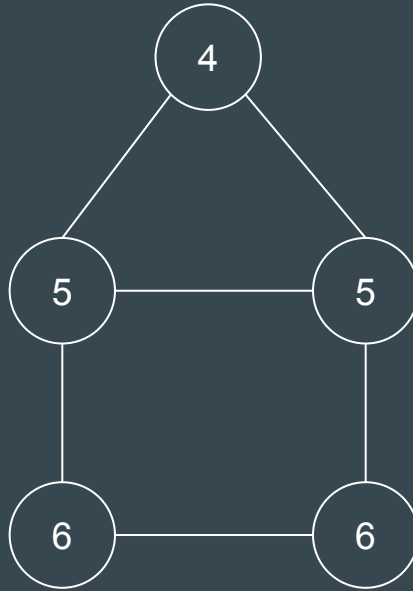


# The WL test for graph isomorphism

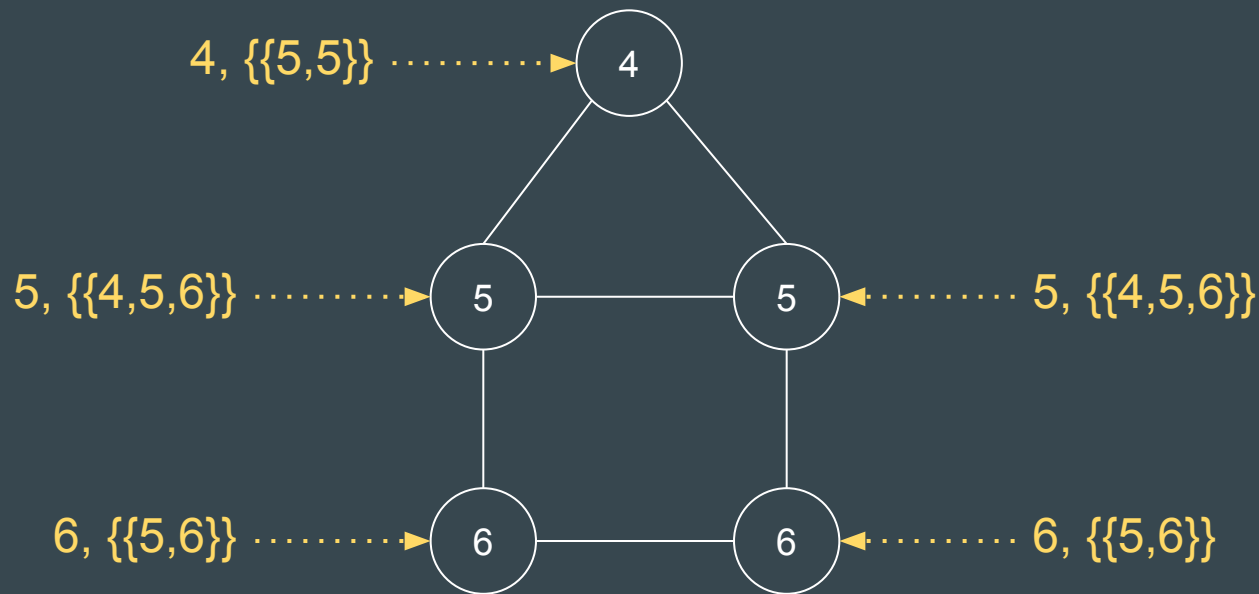




# The WL test for graph isomorphism

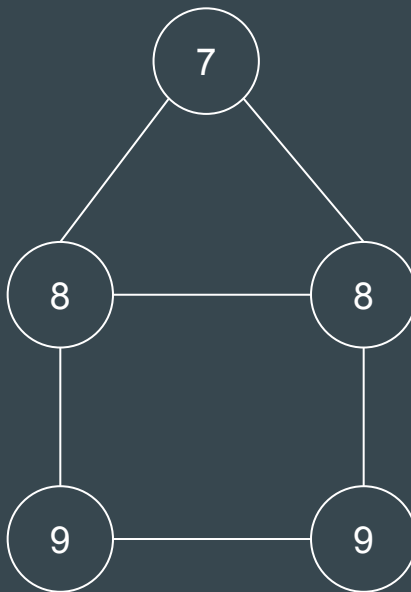


# The WL test for graph isomorphism



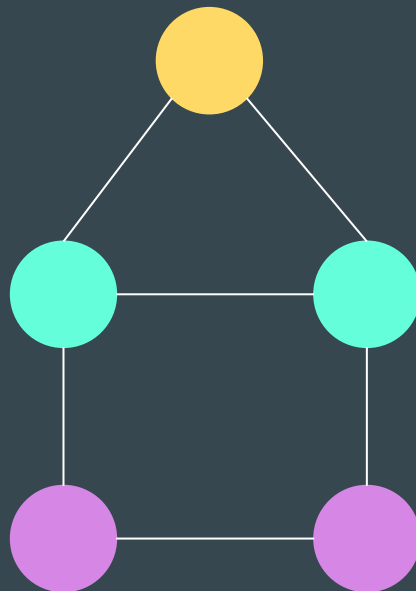
# The WL test for graph isomorphism

We reach a fixpoint



# The WL test for graph isomorphism

The Canonical representation  
(1-dimensional test)



# The WL test and GNNs

The WL test can be considered as a heuristic to verify whether two graph are isomorphic

- But a very good heuristic, with theoretical guarantees

The WL test obviously resembles the way in which GNNs work

**Theorem [Morris et al. 2019, Xu et al. 2019]:** If WL assigns the same color to  $u$  and  $v$  in a graph  $G$ , then every (aggregate-combine) GNN classifies  $u$  and  $v$  in the same way on input  $G$

# The WL test and FO

Consider the fragment  $\text{FOC}^2$  of FO:

$\text{Person}(x) \wedge \exists y [\text{rides}(x,y) \wedge \text{Bus}(y) \wedge \exists x (\text{rides}(x,y) \wedge \text{Infected}(x))]$

$\text{Person}(x) \wedge \exists^{\geq 2} y [\text{rides}(x,y) \wedge \text{Bus}(y) \wedge \exists x (\text{rides}(x,y) \wedge \text{Infected}(x))]$

$\text{FOC}^2$  can be efficiently evaluated as shown before (using only binary tables)

**Theorem [Cai et al. 1992]:** WL assigns the same color to  $u$  and  $v$  in a graph  $G$  if and only if either  $u,v \in Q(G)$  or  $u,v \notin Q(G)$ , for every unary query  $Q(x)$  in  $\text{FOC}^2$

## Putting all together

**Theorem [Barceló et al. 2020]:** There exists a (natural) fragment of  $\text{FOC}^2$  with the same expressive power as (aggregate-combine) GNNs

Such a fragment of  $\text{FOC}^2$  includes the previous formulae:

$$\text{Person}(x) \wedge \exists y [\text{rides}(x,y) \wedge \text{Bus}(y) \wedge \exists x (\text{rides}(x,y) \wedge \text{Infected}(x))]$$
$$\text{Person}(x) \wedge \exists^{\geq 2} y [\text{rides}(x,y) \wedge \text{Bus}(y) \wedge \exists x (\text{rides}(x,y) \wedge \text{Infected}(x))]$$

## Some questions to think about

Can learning techniques for GNNs be used for learning queries on graphs?

- What are good algorithms for translating (aggregate-combine) GNNs into (well-studied) declarative query languages?

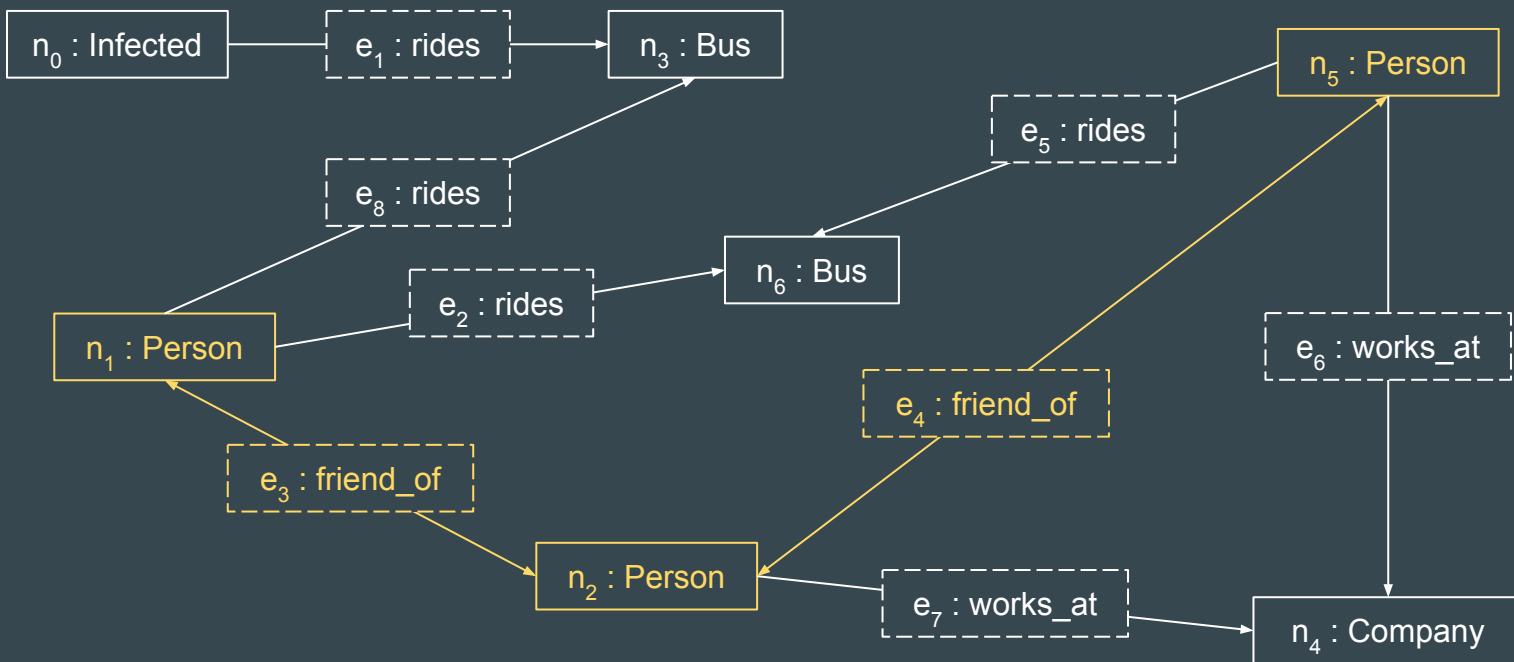
What is the appropriate GNN architecture for regular expressions?

- A form of recursion need to be included



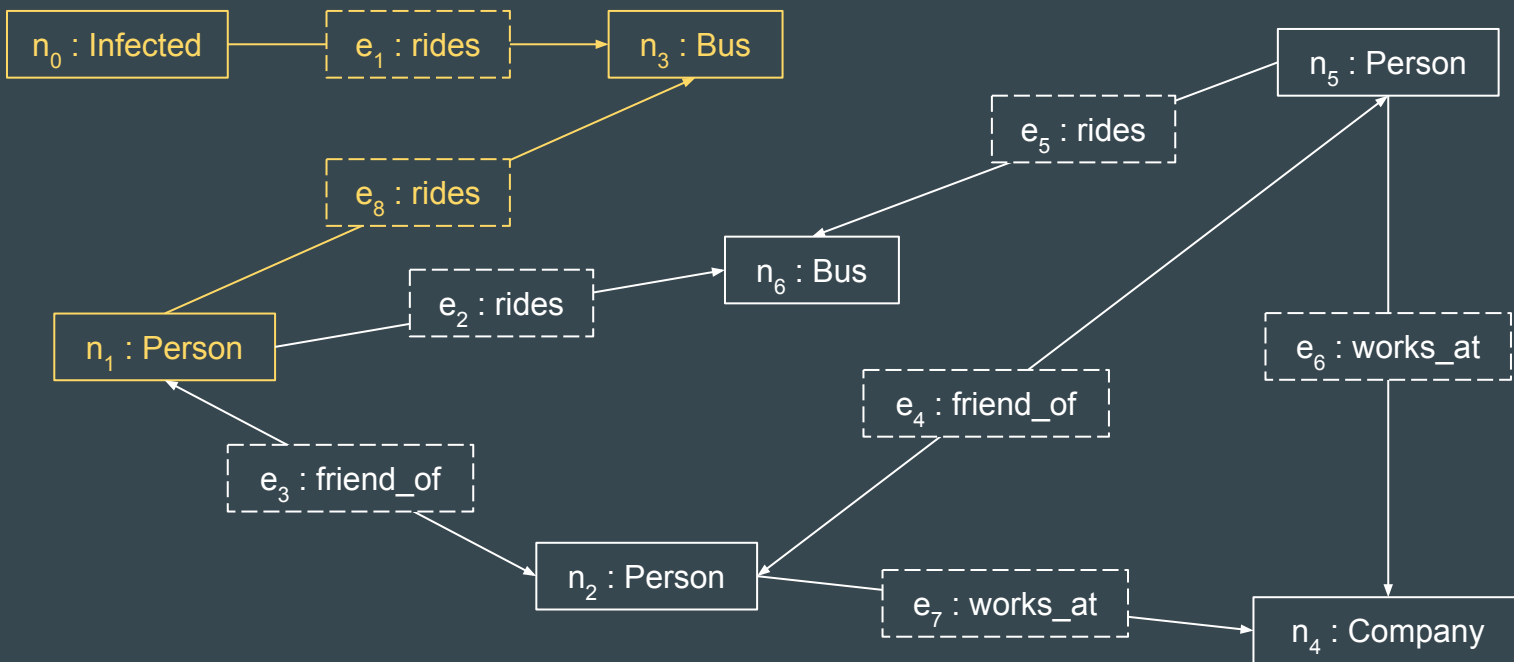
# Extracting paths from a graph: also an old problem

A canonical example: `?Person/(friend_of/?Person)+`



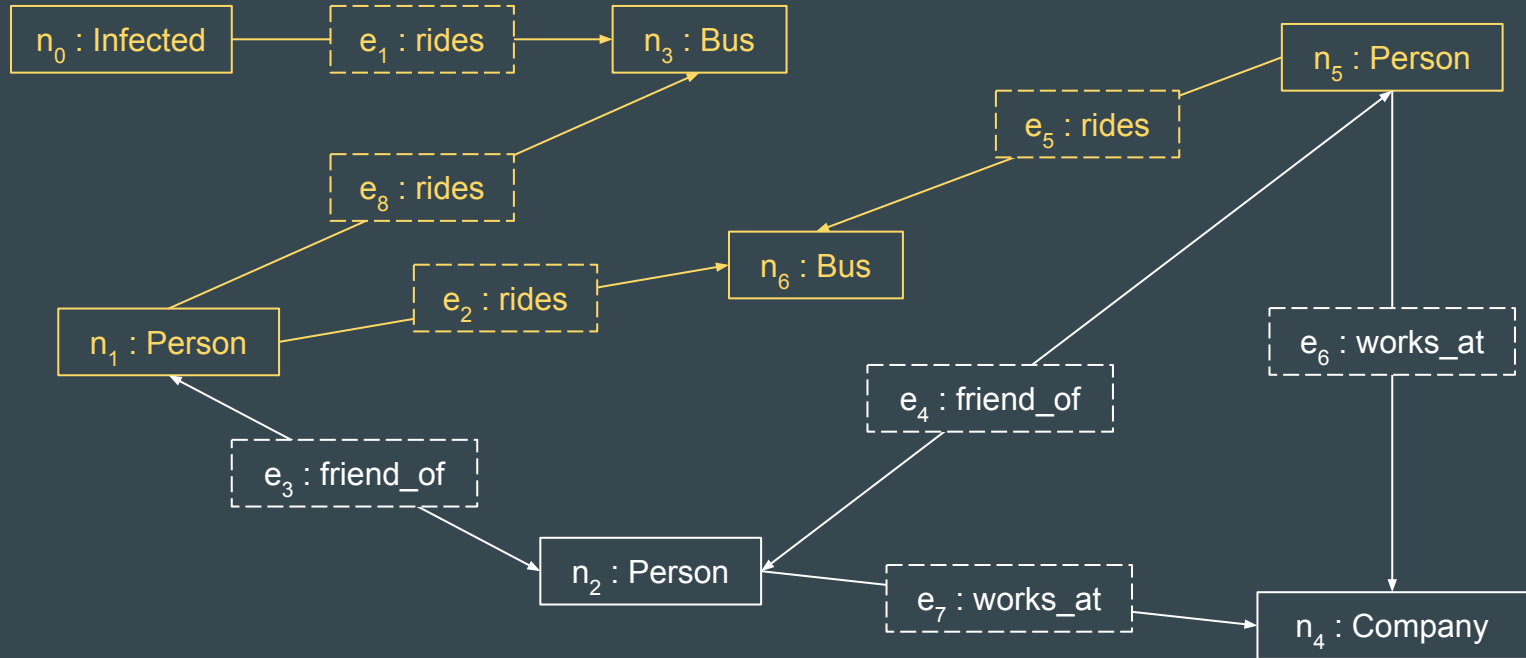
# Extracting paths from a graph: also an old problem

The notion of close contact: `?Infected/rides/?Bus/rides~/?Person`



# Extracting paths from a graph: also an old problem

A stricter notion of close contact:  $?Infected/(rides/?Bus/rides^-/?Person)^+$



# A new approach to an old problem

Give up completeness: we do not want to find *all* paths that conforms to a regular expression, even if their length is given as parameter

We consider problems:

- **COUNT( $G, r, n$ )**: count the number of paths  $p$  in  $G$  such that  $p$  conforms to  $r$  and the length of  $p$  is  $n$
- **GEN( $G, r, n$ )**: generate uniformly at random a path  $p$  in  $G$  such that  $p$  conforms to  $r$  and the length of  $p$  is  $n$

# Are these difficult problems?

Without including regular expressions as parameter,  $\text{COUNT}(G, n)$  can be solved efficiently by a dynamic programming approach

$\text{COUNT}(G, r, n)$  is #P-complete

- If it can be solved in polynomial time, then  $P = NP$

How do we solve the previous problems? Give up precision

# Randomized approximation to the rescue

#P-hardness of  $\text{COUNT}(G, r, n)$  does not preclude the existence of an approximation algorithm for this problem

We would like to have an algorithm  $A(G, r, n, \epsilon)$  that approximates  $\text{COUNT}(G, r, n)$  with a relative error  $\epsilon$

- It should run in time polynomial in  $|G| + |r| + n$  and in  $1/\epsilon$

# Randomized approximation to the rescue

But we would also need randomization in this case.

We ask  $A(G, r, n, \epsilon)$  to be a fully polynomial-time randomized approximation scheme:

$$\Pr \left( \left| \frac{\text{COUNT}(G, r, n) - A(G, r, n, \epsilon)}{\text{COUNT}(G, r, n)} \right| \leq \epsilon \right) \geq 1 - \frac{1}{2^{100}}$$

and  $A(G, r, n, \epsilon)$  runs in time  $\text{poly}(|G|, |r|, n, 1/\epsilon)$

# Randomized approximation to the rescue

**Theorem [Arenas et al. 2019]:** There exists a fully polynomial-time randomized approximation scheme for  $\text{COUNT}(G, r, n)$

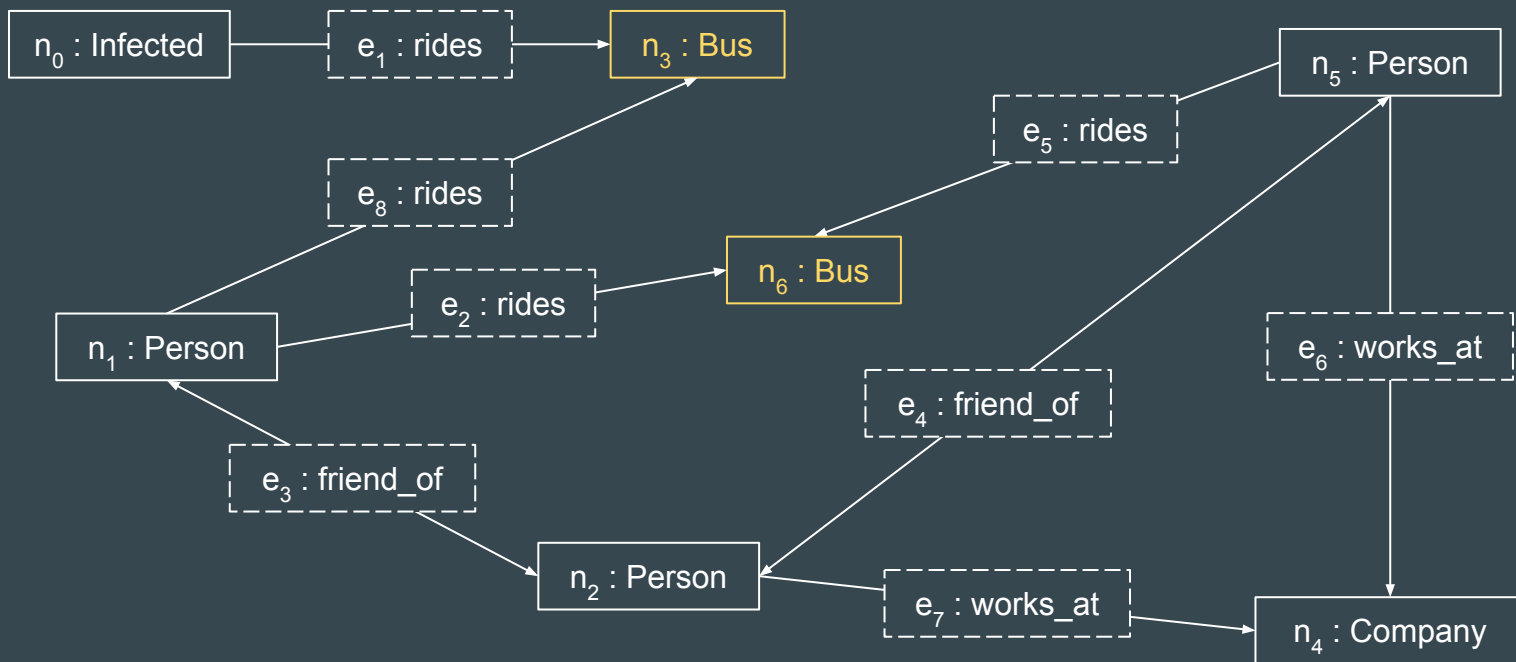
Such a schema can be used to provide a randomized algorithm for  $\text{GEN}(G, r, n)$

- Samples can be generated efficiently with an *almost* uniform distribution



# An application to global properties

How important is a bus service?



# Betweenness centrality of a node in a graph

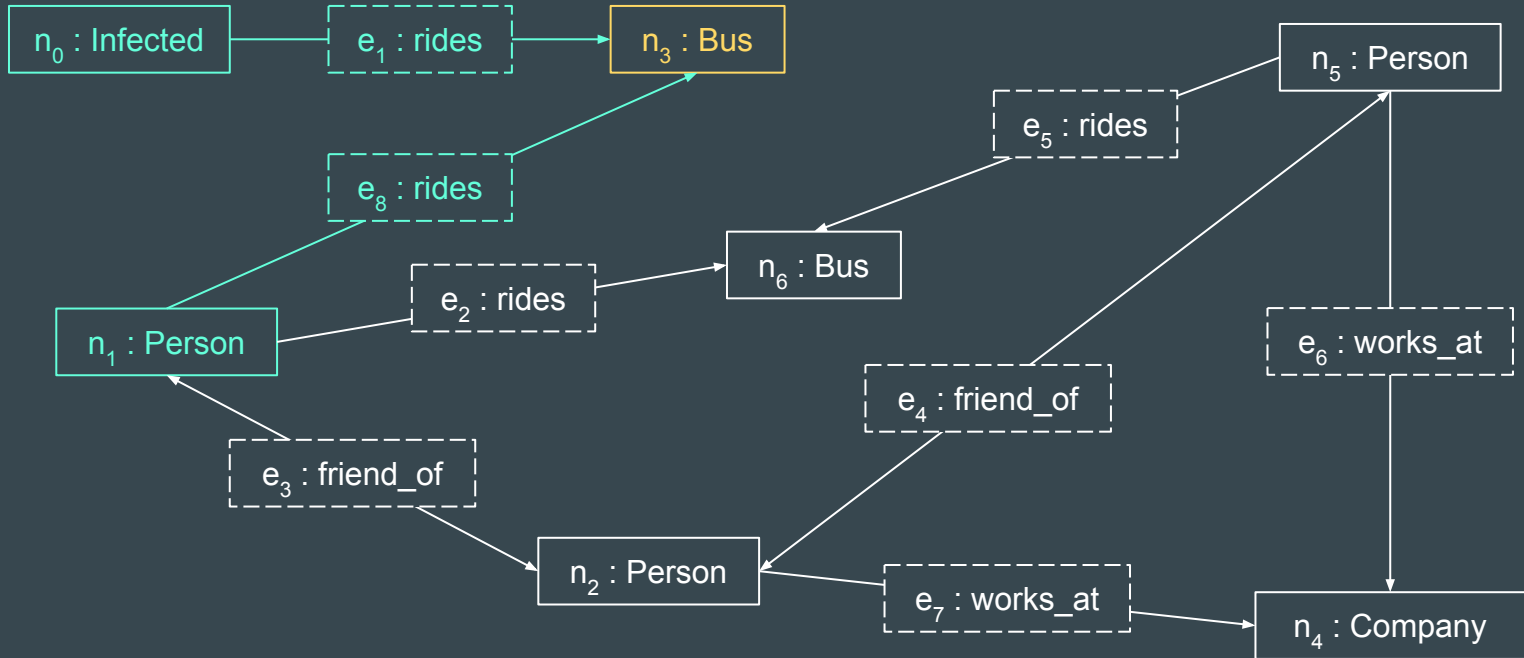
- $S_{a,b}$  : set of shortest paths from  $a$  to  $b$  in  $G$
- $S_{a,b}(u)$  : set of paths in  $S_{a,b}$  that include node  $u$

$$bc(u) = \sum_{\substack{a, b \\ a \neq u \wedge b \neq u}} \frac{|S_{a,b}(u)|}{|S_{a,b}|}$$

Betweenness centrality can be computed in polynomial time.

# Is betweenness centrality the appropriate notion?

How important is a bus service in the spread of a communicable disease?



# Restricting paths in betweenness centrality

- $S_{a,b,r}$ : set of shortest paths from  $a$  to  $b$  in  $G$  that conforms to regular expression  $r$
- $S_{a,b,r}(u)$ : set of paths in  $S_{a,b,r}$  that include node  $u$

$$bc_r(u) = \sum_{\substack{a, b \\ a \neq u \wedge b \neq u}} \frac{|S_{a,b,r}(u)|}{|S_{a,b,r}|}$$

Can this notion of centrality be computed in polynomial time?

## Randomized approximation again to the rescue

Use previous algorithm to approximate  $|S_{a,b,r}(u)|$  and  $|S_{a,b,r}|$

- For example, with errors  $\epsilon^2/4$  and  $\epsilon/4$  for  $|S_{a,b,r}(u)|$  and  $|S_{a,b,r}|$ , respectively

The you get an approximation of  $bc_r(u)$  with error  $\epsilon$  that can be computed in polynomial time.

# Paths should be treated as first-class citizens

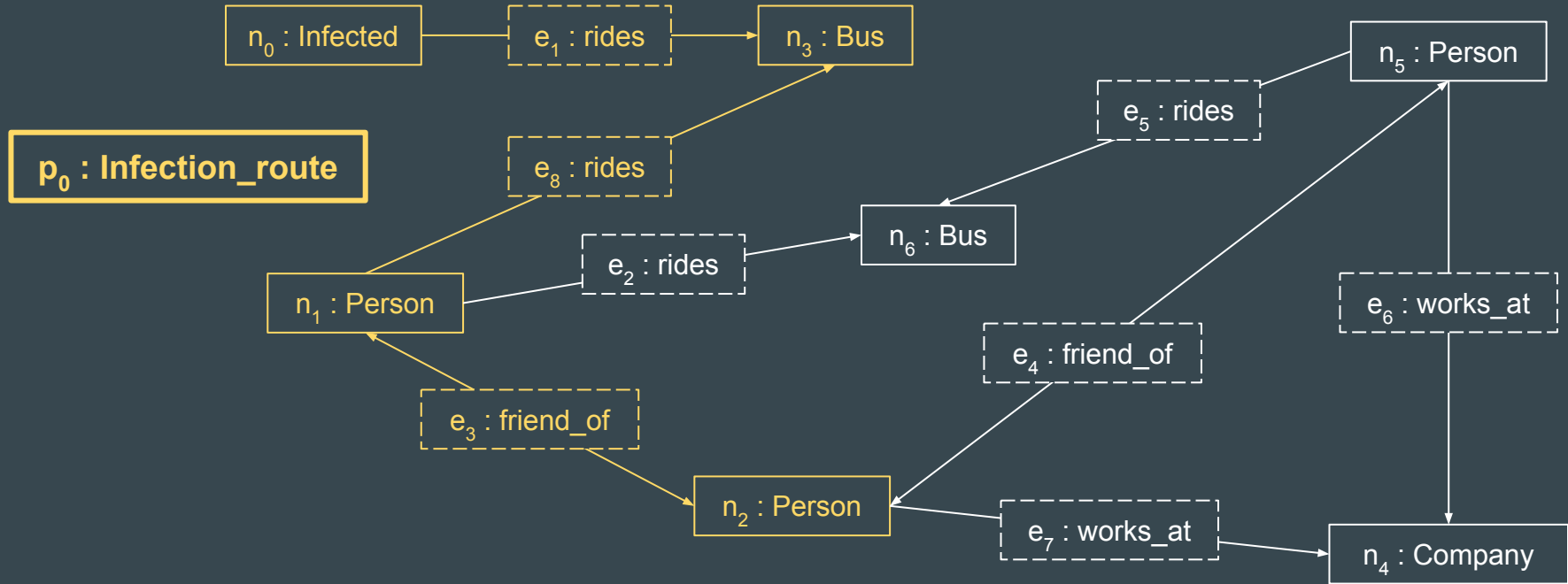
Treated at the same level as nodes and edges, so that paths can

- be materialized and stored
- have labels
- have values for properties, or associated vectors of features

The previous centrality measure can be formulated as a query over a set of paths

- Such set of paths can be defined by a sub-query

# Paths as first-class citizens



# Some questions to think about

Can a fully polynomial-time randomized approximation scheme for COUNT be effectively used in practice?

- Can be used to provide *fair* answers in practice?

How can centrality measures be adapted to deal with knowledge graphs?

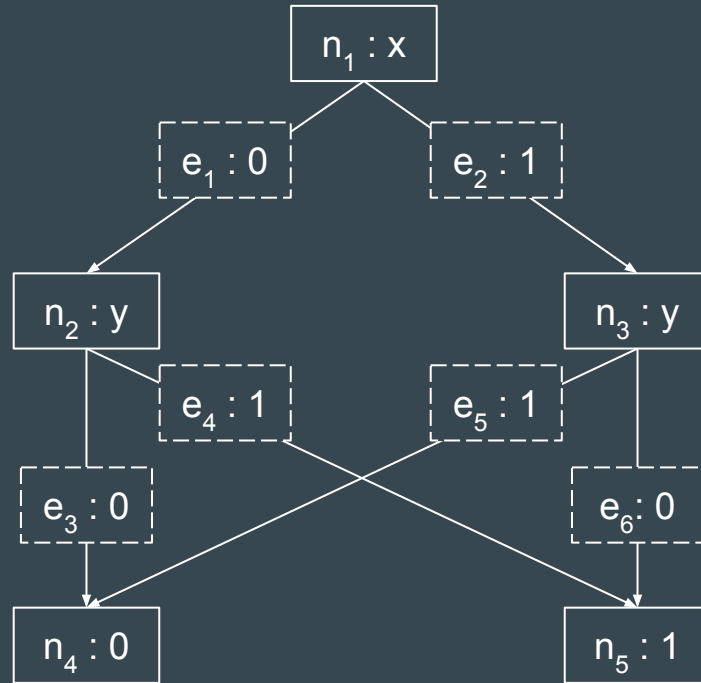
- What is an appropriate definition of a centrality measure that takes labels into account?

How can paths be included as first class citizens in a query language?

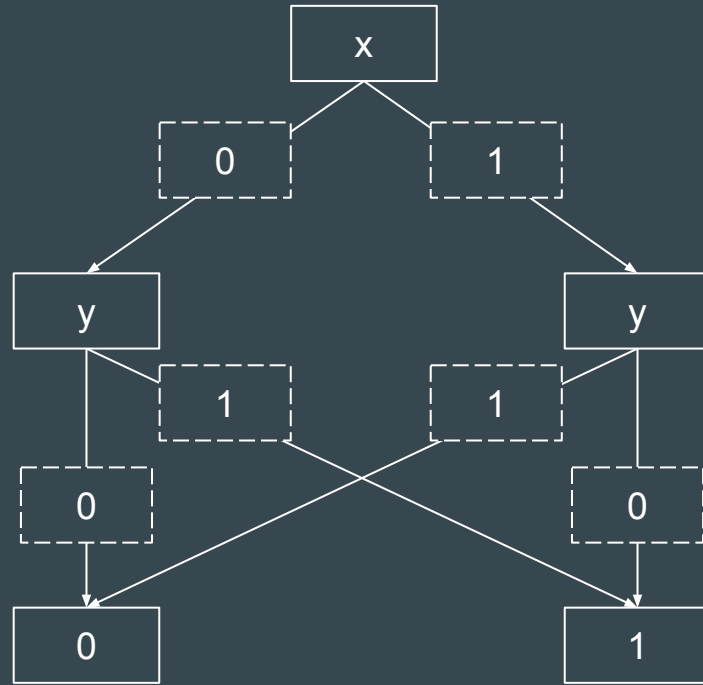
- A proposal in the query language G-CORE introduced in [Angles et al. 2018]



# A step beyond: global properties and explainable AI



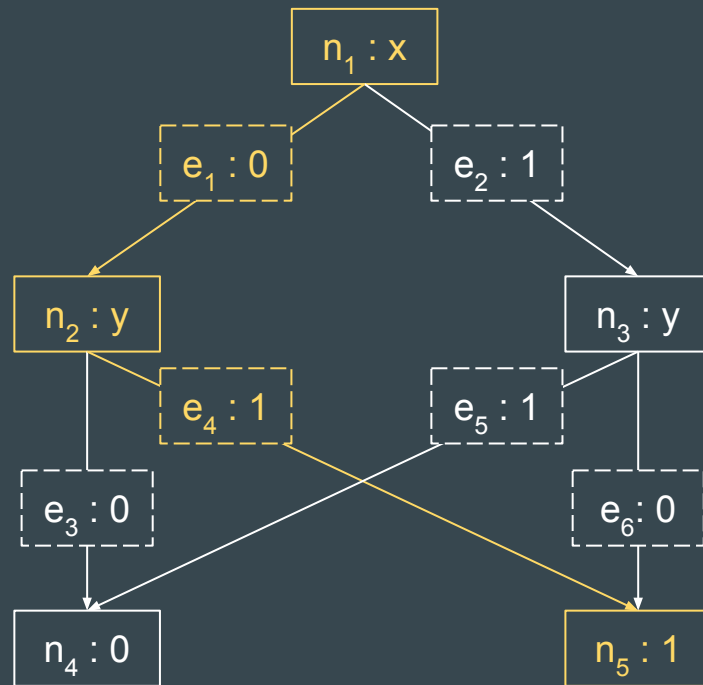
# A step beyond: global properties and explainable AI



# What kind of queries should we answer?

Is there any instance that is classified positively?

Is there any instance that is classified negatively?

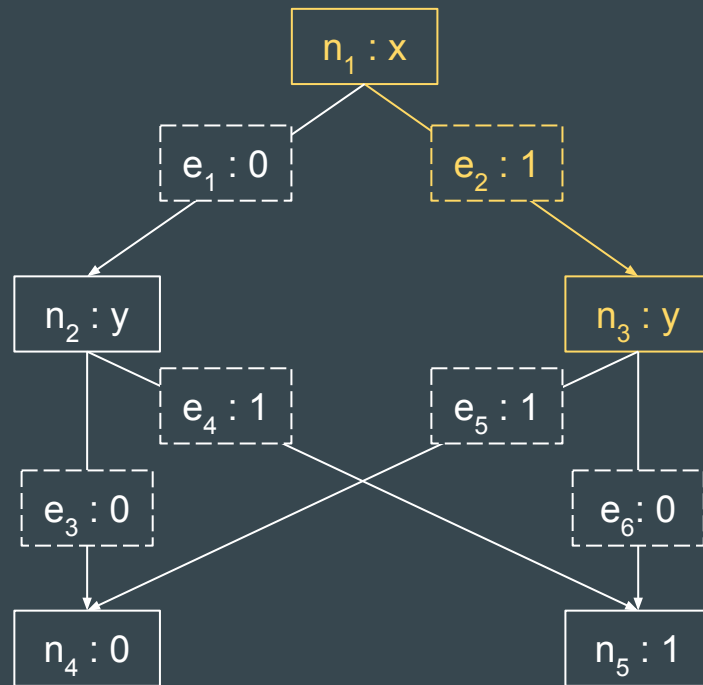


# What kind of queries should we answer?

Is there a completion of  $x \mapsto 1$  that is classified positively?

Are all the completion of  $x \mapsto 1$  classified positively?

- So that  $x \mapsto 1$  is a sufficient reason for the positive value

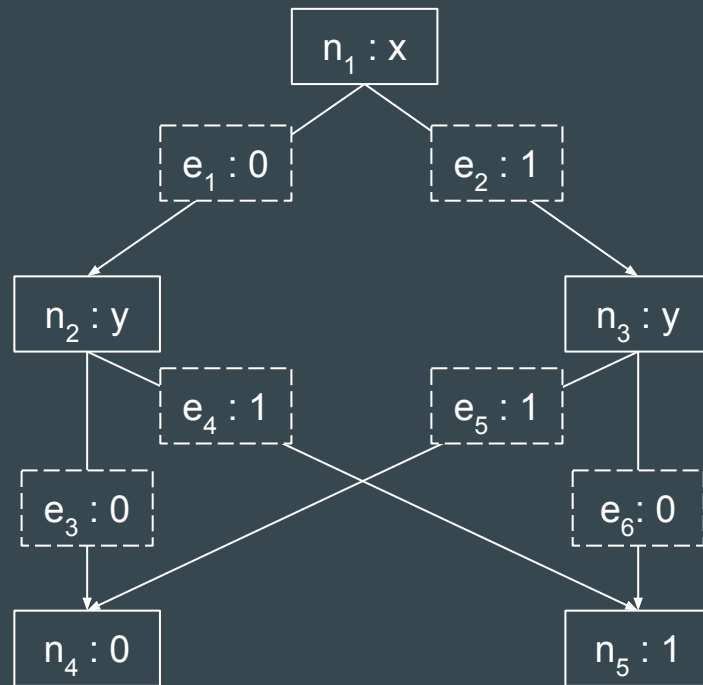


# A declarative language for model interpretability

Given an instance classified positively,  
what is a sufficient reason for it?

What is a minimal sufficient reason for this  
instance?

Is the model biased with respect to a  
protected feature?



## Some questions to think about

How can a declarative language for model interpretability be defined?

Can such a language be based on *path expressions*? How can such expressions be combined with *quantifiers*?

Can such a language be evaluated efficiently?

- How does this evaluation depend on the structure of the graph? Models can be decision trees, OBDDs, FBDDs, ...

**We have gone through technical challenges.  
Is that all?**

...

# Topics we did not cover

At least we are aware of:

- Human visualization of graphs (Upcoming Dagstuhl-Seminar 22031)
- HCI aspects of graph query languages
- Storing and infrastructure issues
- Enterprise and organizational issues
- Governance issues
- Ethical issues

**Message: querying is not only a formal / technical topic**



# Important reminder: humans are always in the loop

<b>Context</b>	<b>Trend</b>	<b>Organizational Need</b>	<b>Technology</b>	<b>Role</b>
Web + Moore's Law	Big Data	Harness and collect data	Commodity distributed computing platforms (e.g. Hadoop)	<b>Data Engineer</b>
Big Data + GPU Compute	AI Revolution	Draw value from data	Commodity machine learning (e.g., TensorFlow, SciPy)	<b>Data Scientist</b>
AI Revolution + Cloud Computing	Data-Driven Organization, Digital Transformation	Rely on data	Clean, meaningful, data technologies (e.g. knowledge graphs, data wrangling systems, data catalog platforms)	<b>?</b>

# Important reminder: humans are always in the loop

Context	Trend	Organizational Need	Technology	Role
Web + Moore's Law	Big Data	Harness and collect data	Commodity distributed computing platforms (e.g. Hadoop)	<b>Data Engineer</b>
Big Data + GPU Compute	AI Revolution	Draw value from data	Commodity machine learning (e.g., TensorFlow, SciPy)	<b>Data Scientist</b>
AI Revolution + Cloud Computing	Data-Driven Organization, Digital Transformation	Rely on data	Clean, meaningful, data technologies (e.g. knowledge graphs, data wrangling systems, data catalog platforms)	<b>Knowledge Scientist</b>

## Data is a Team Sport



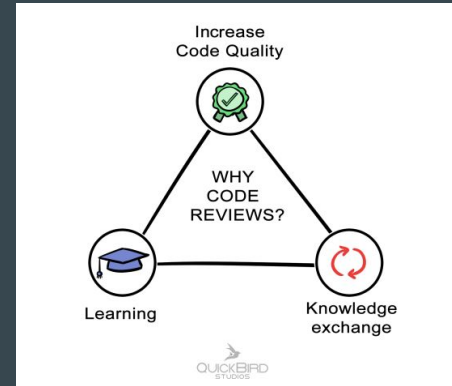
## The most important data isn't data



## Agile Data Development



## Data Review





## Knowledge Report

### Knowledge Capture

1. Analyze as-is process
2. Collect Documentation
3. Develop Knowledge Report



### Business Question

## Pay-as-you-go Methodology

### Knowledge Implementation

4. Create/Extend Knowledge Graph Schema
5. Implement Mapping
6. Generate Data Products
7. Validate Data



### Enterprise Knowledge Graph



### Business Answer

### Knowledge Access

8. Build Report
9. Answer Business Question
10. Move to Production

[Sequeda et al. 2019]

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[Sequeda et al. 2019] J. F. Sequeda, W. J. Briggs, D. P. Miranker, and W. P. Heideman. *A Pay-as-you-go Methodology to Design and Build Enterprise Knowledge Graphs from Relational Databases*. ISWC 2019.

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# Takeaways

- Graphs are not just another data model
  - They have always been here
  - They are not going away
  - This is the right time. We are lucky to be here!
- Knowledge Graphs are more than just graph databases
- Exciting to see results from different areas getting connected
  - Connection of Graph Neural Networks and Graph Query Languages
- Opportunities
  - Explainable AI and the search of a declarative language for interpretability
- Computing is approaching the fine line separating technology from humans. We should be open to learning from other disciplines.